



Collisionless Dark Matter Spikes:

Open questions in formation, evolution and gravitational wave detection

Bradley J. Kavanagh (IFCA, CSIC-UC)

EuCAPT Workshop: GW probes of BH environments
Rome, 16 June 2022



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EXCELENCIA
MARÍA
DE MAEZTU



CSIC

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A broad effort

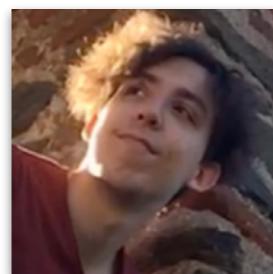
Gianfranco Bertone
(GRAPPA, Amsterdam)



Pratibha Jangra
(IFCA, Santander)



Pippa Cole
(GRAPPA, Amsterdam)



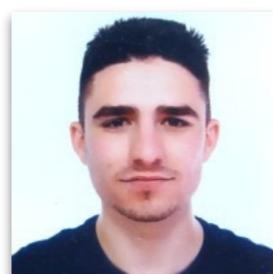
Adam Coogan
(Mila, Montreal)



Jose Maria Diego
(IFCA, Santander)



David Nichols
(U. Virginia)



Daniele Gaggero
(IFIC, Valencia)



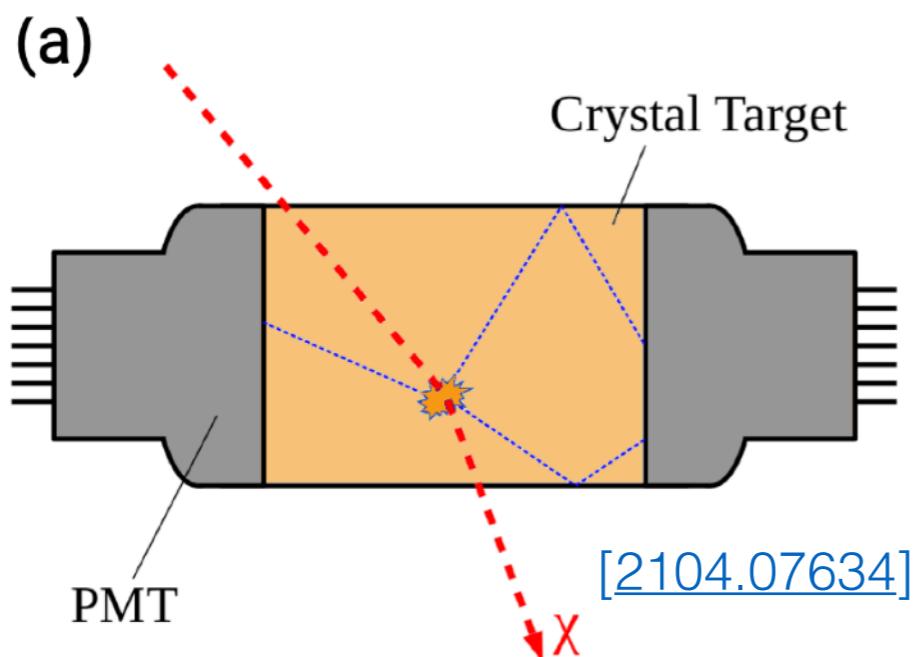
Abram Perez Herrero
(IFCA, Santander)



Francesca Scarcella
(IFT, Madrid)

...and many others...

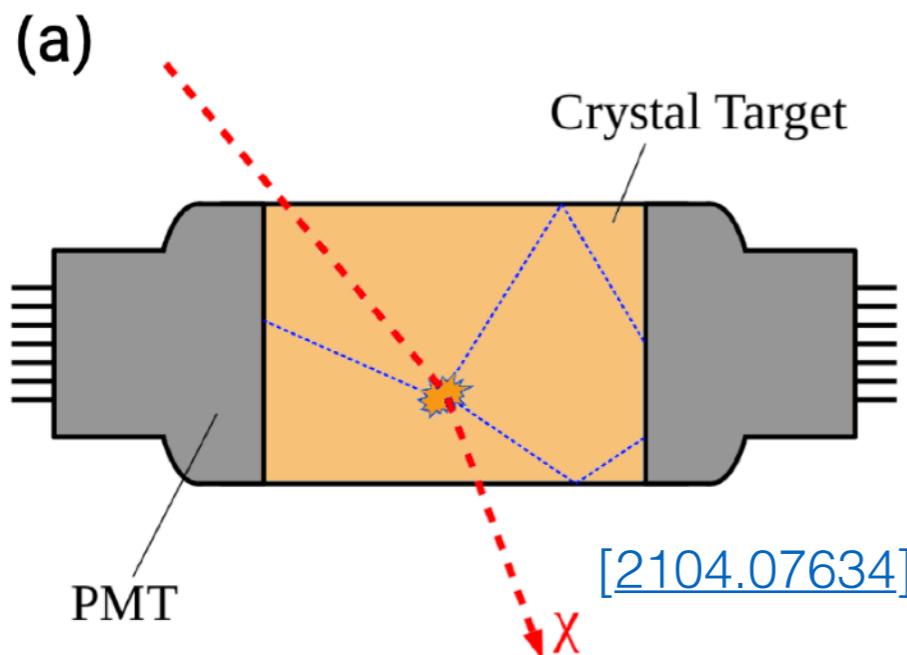
Searches for Dark Matter in the Galactic Halo



$$\rho_{\text{DM}} \sim 10^{-2} M_{\odot} \text{ pc}^{-3}$$

[Read, [1404.1938](#)]

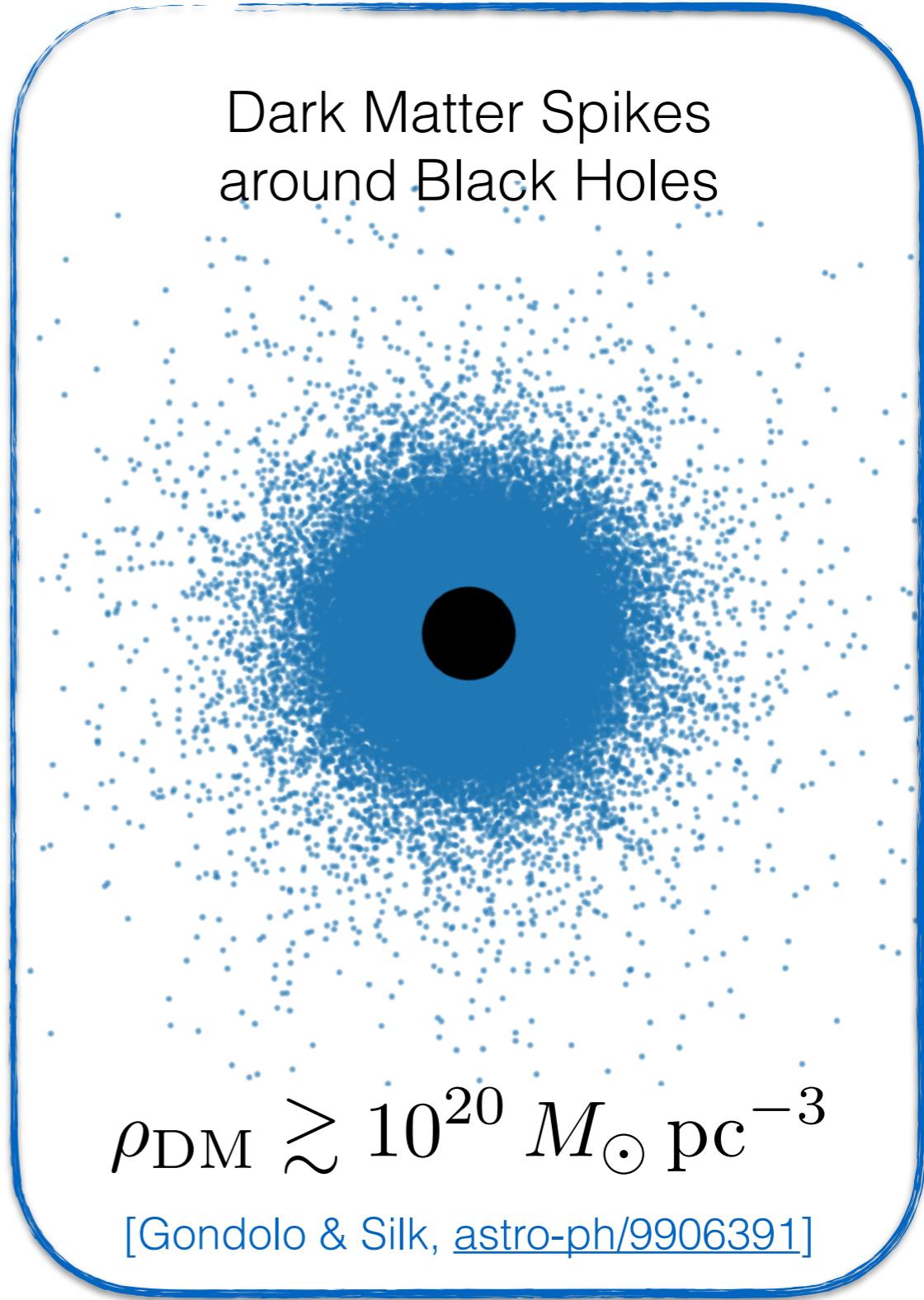
Searches for Dark Matter in the Galactic Halo



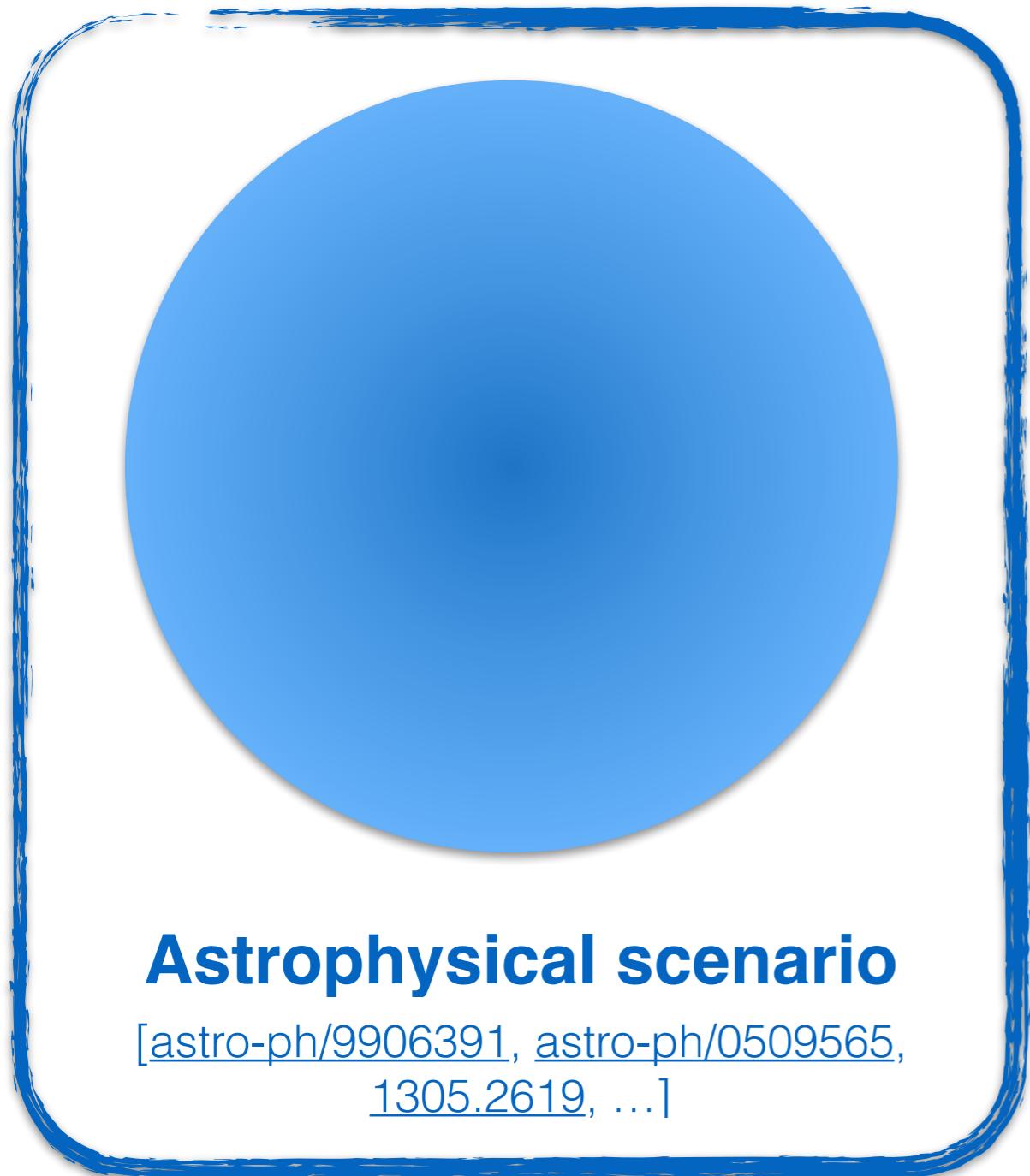
$$\rho_{\text{DM}} \sim 10^{-2} M_{\odot} \text{ pc}^{-3}$$

[Read, [1404.1938](#)]

Dark Matter Spikes around Black Holes



Collisionless **DM ‘spike’** or **‘dress’** around an **IMBH**:

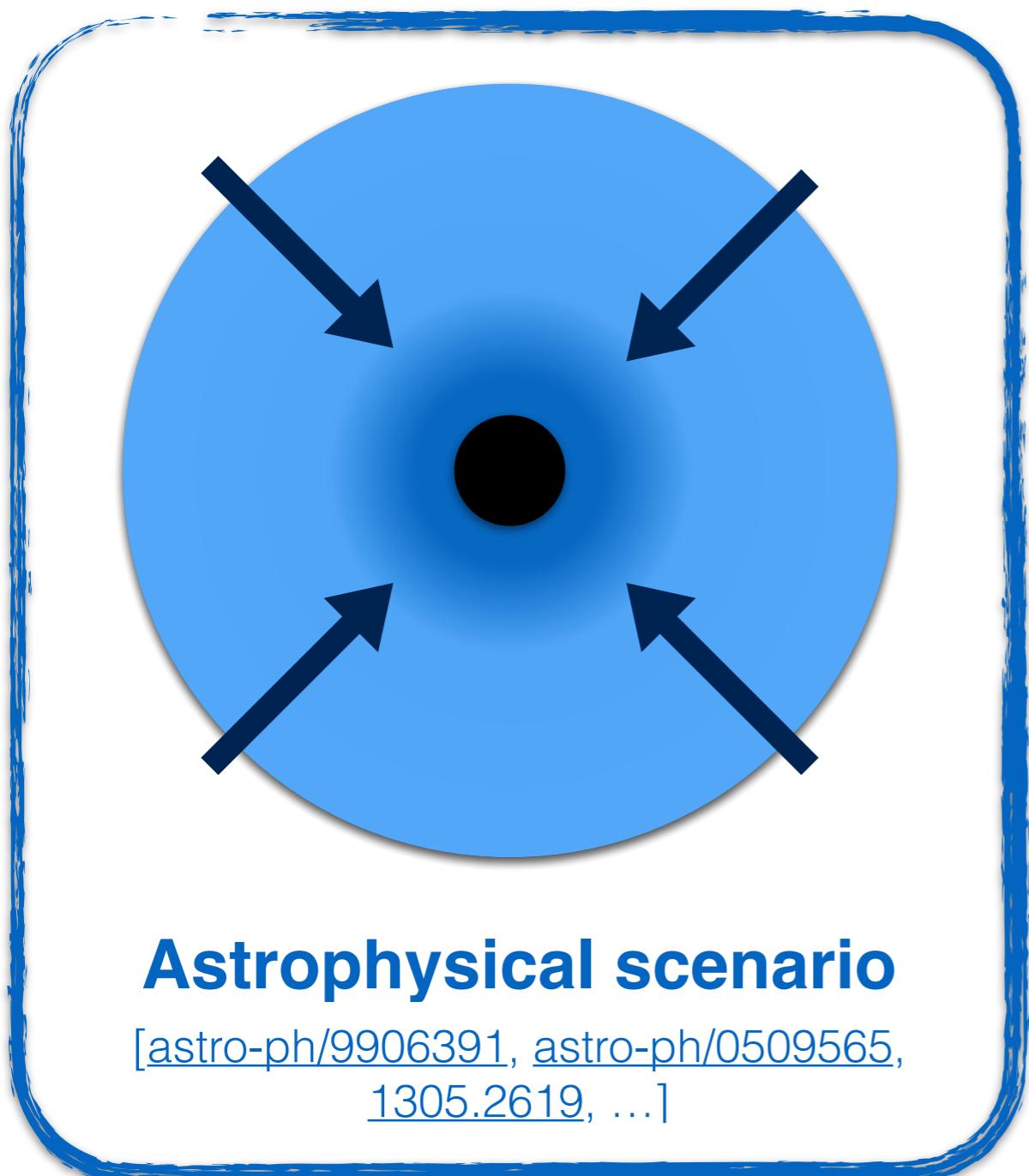


Astrophysical scenario

[[astro-ph/9906391](#), [astro-ph/0509565](#),
[1305.2619](#), ...]

More on this later...

Collisionless DM '**spike**' or '**dress**' around an **IMBH**:

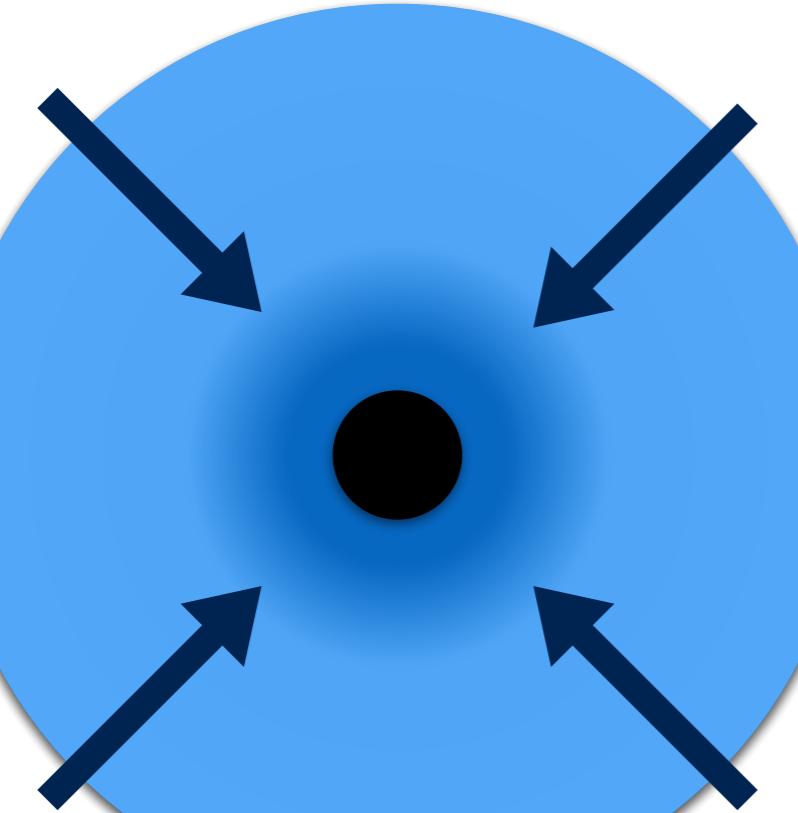


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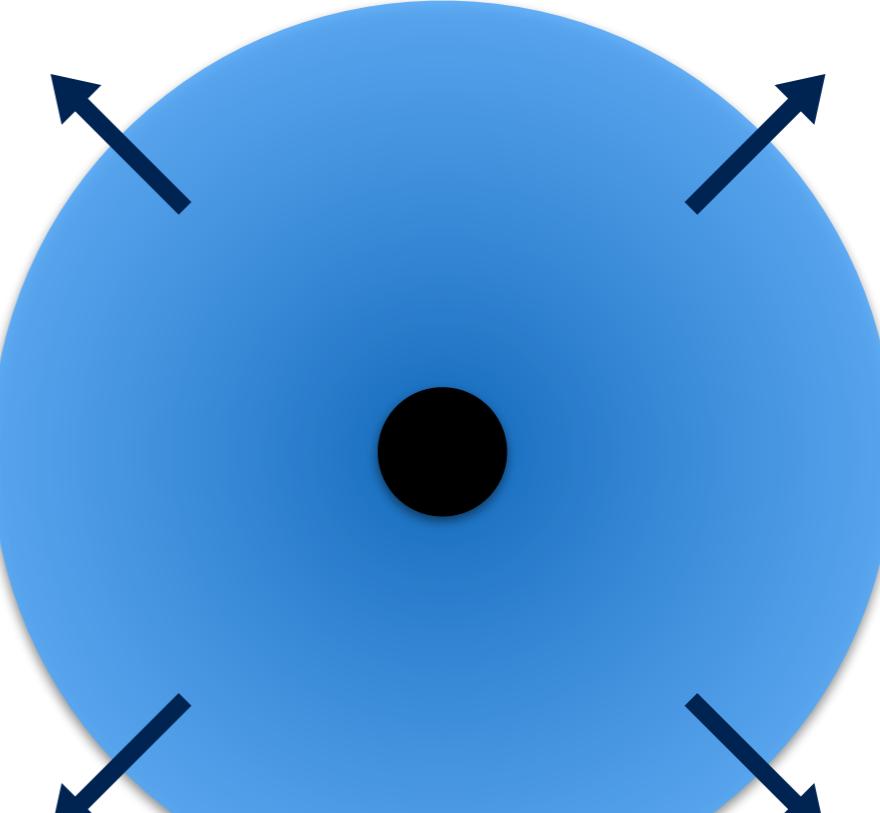
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Collisionless DM ‘**spike**’ or ‘**dress**’ around an **IMBH**:



Astrophysical scenario

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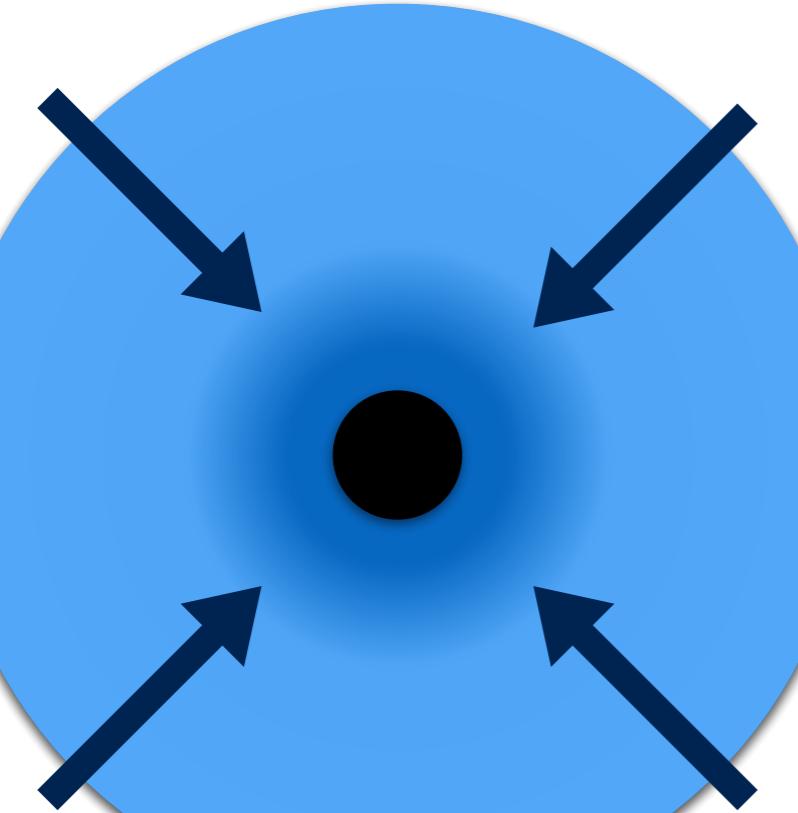


PBH scenario

[[Bertschinger \(1985\)](#), [astro-ph/0608642](#),
[1901.08528](#), ...]

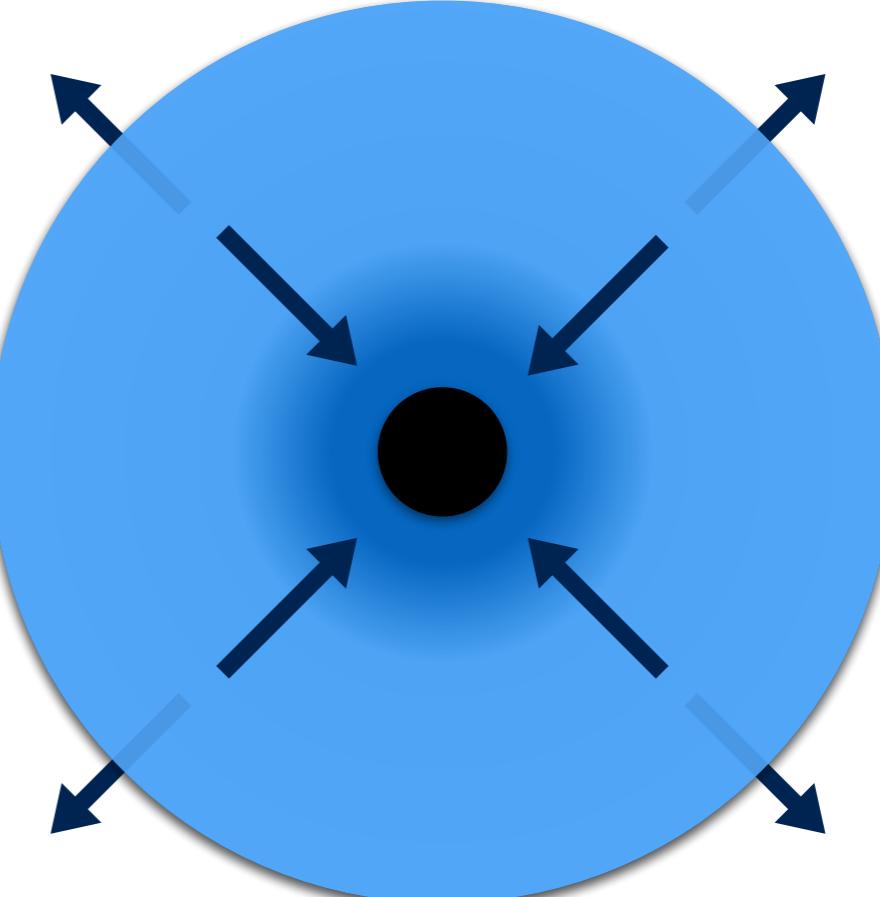
More on this later...

Collisionless DM ‘**spike**’ or ‘**dress**’ around an **IMBH**:



Astrophysical scenario

[[astro-ph/9906391](#), [astro-ph/0509565](#),
[1305.2619](#), ...]



PBH scenario

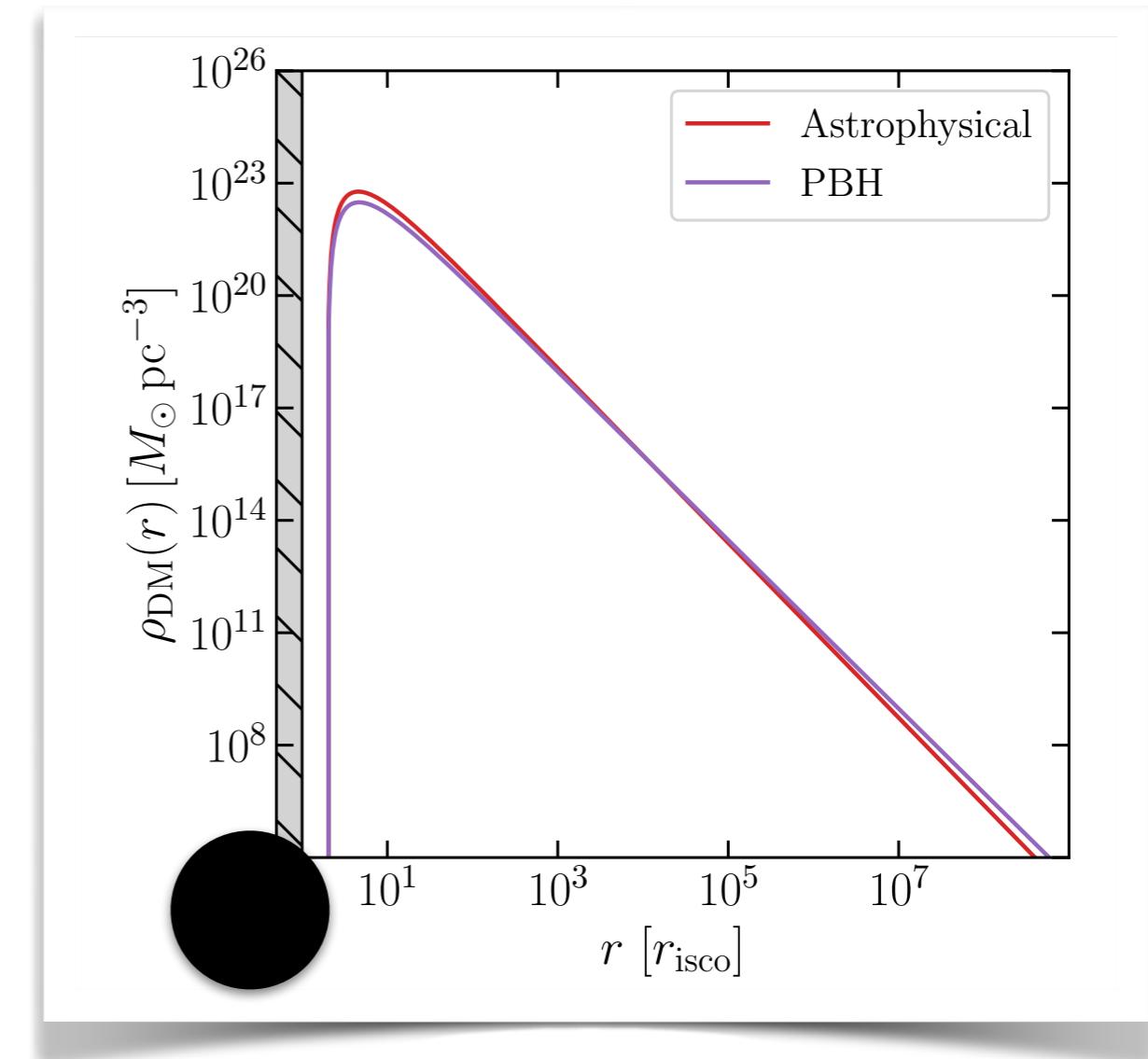
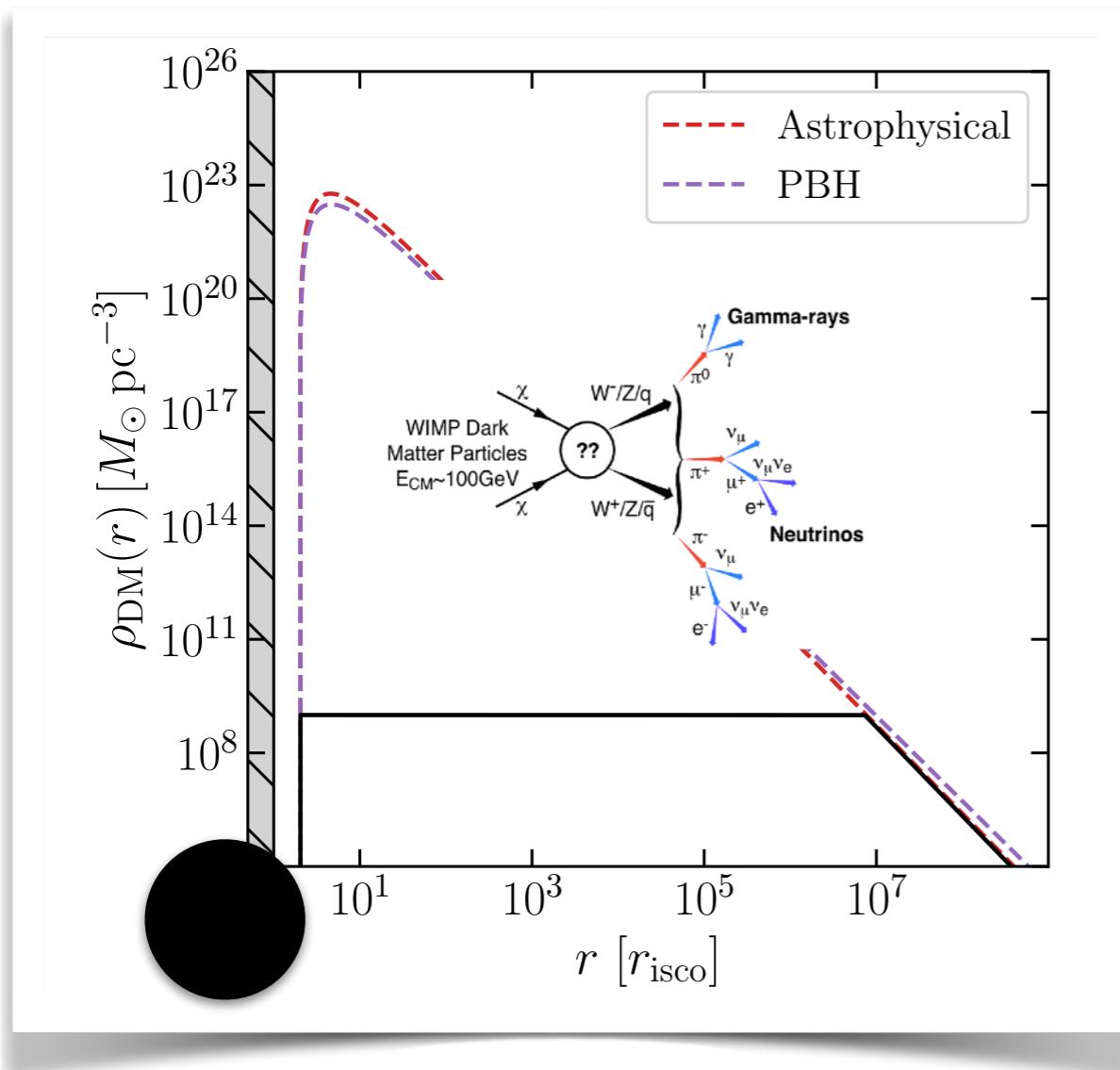
[[Bertschinger \(1985\)](#), [astro-ph/0608642](#),
[1901.08528](#), ...]

More on this later...

Survival of the Spike

$$m_1 = 10^3 M_\odot \quad \rho_{\text{DM}} = \rho_6 \left(\frac{10^{-6} \text{ pc}}{r} \right)^{\gamma_{\text{sp}}} \quad \gamma_{\text{sp}} \sim 2 - 2.5$$

1) DM properties:



[E.g. Bertone, Coogan, Gaggero, **BJK** & Weniger, [1905.01238](#)]

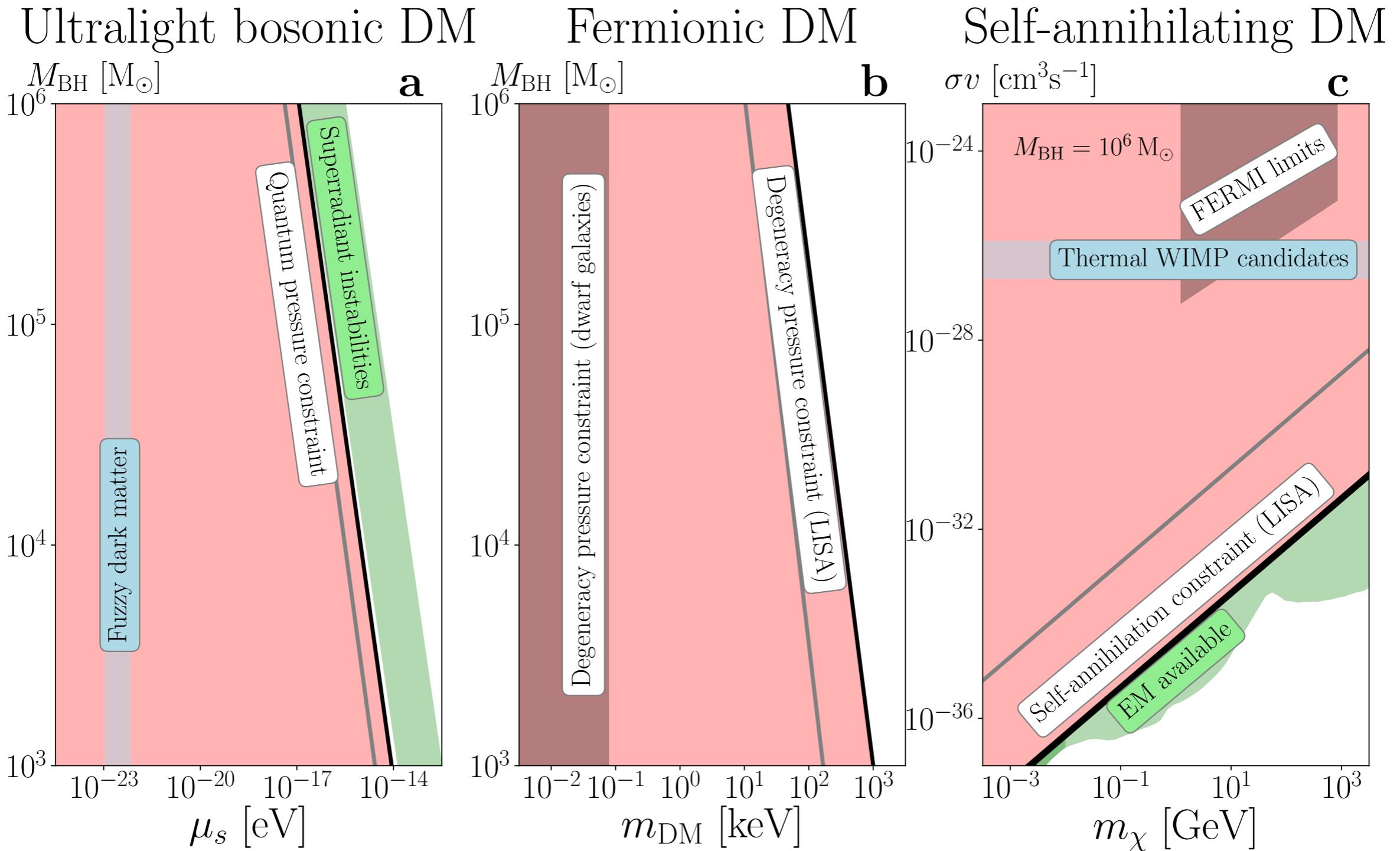
2) BH environment: Need a quiet life for the BH, not too many major mergers

[E.g. Bertone & Merritt, [astro-ph/0501555](#)]



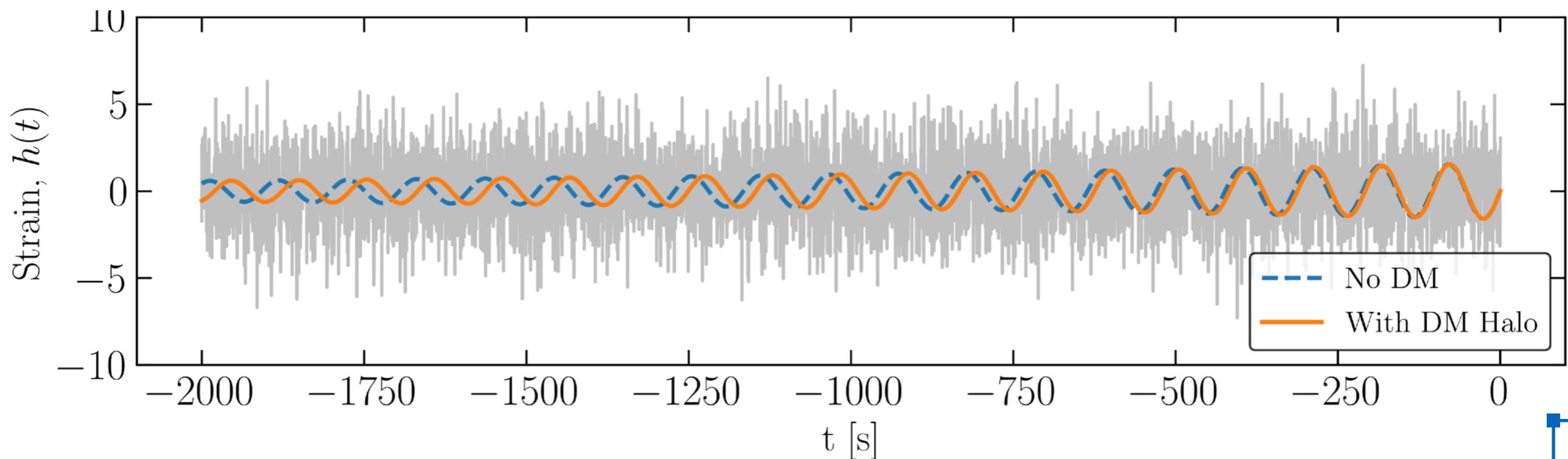
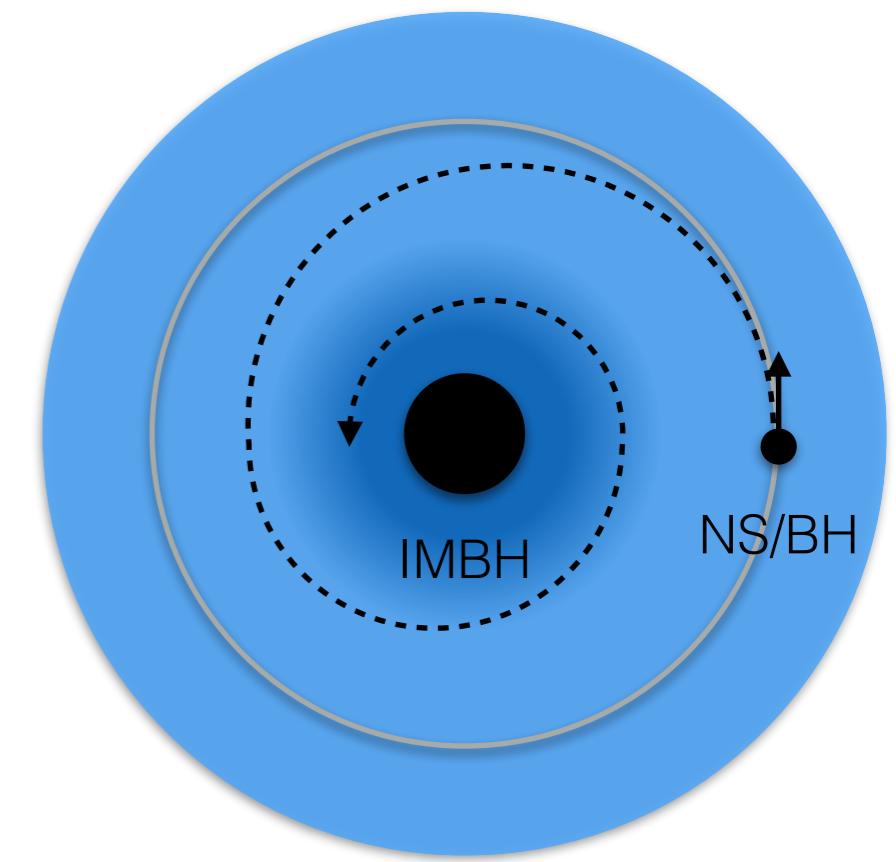
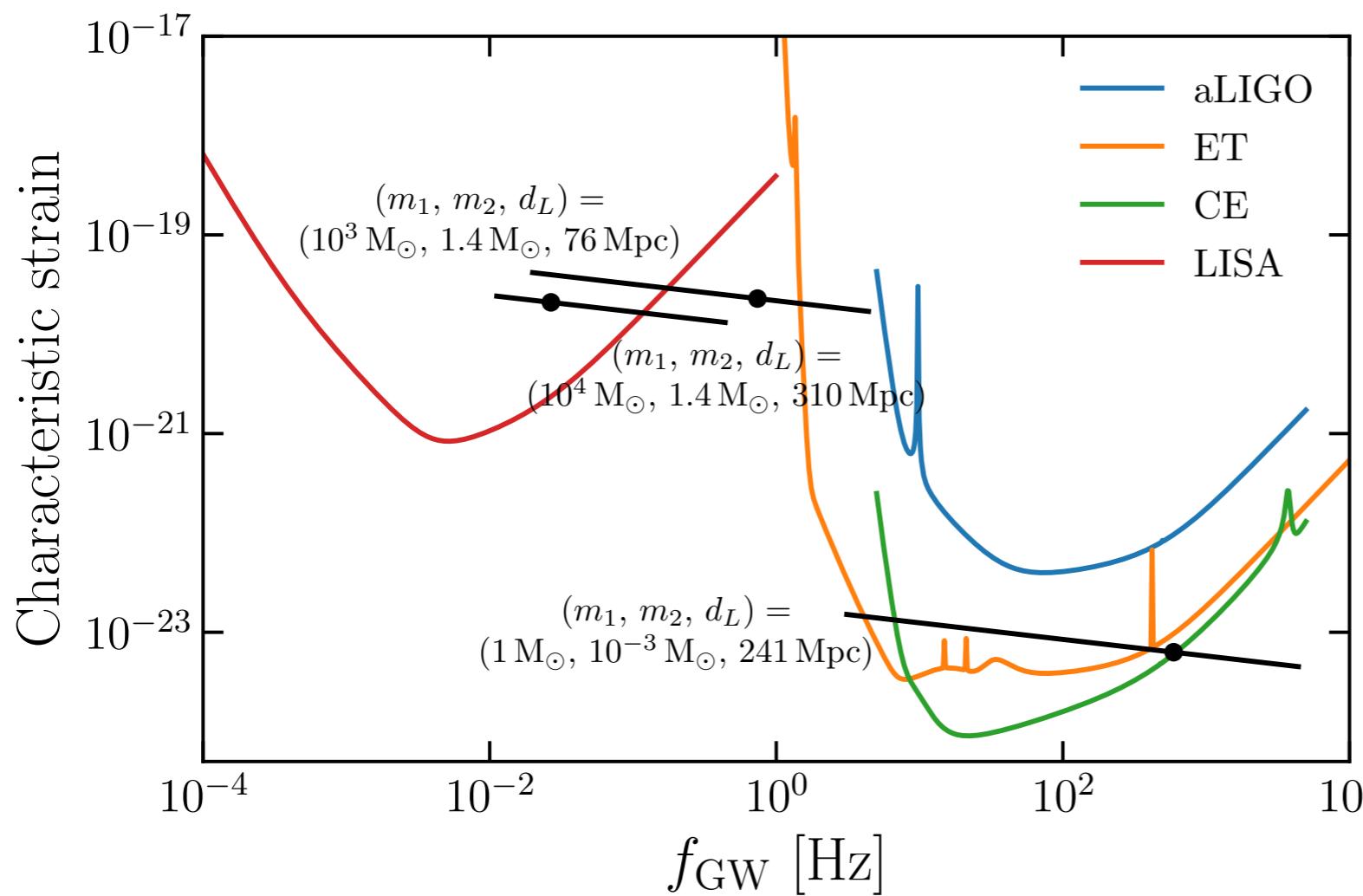
Focus on IMBHs

Nature of Dark Matter

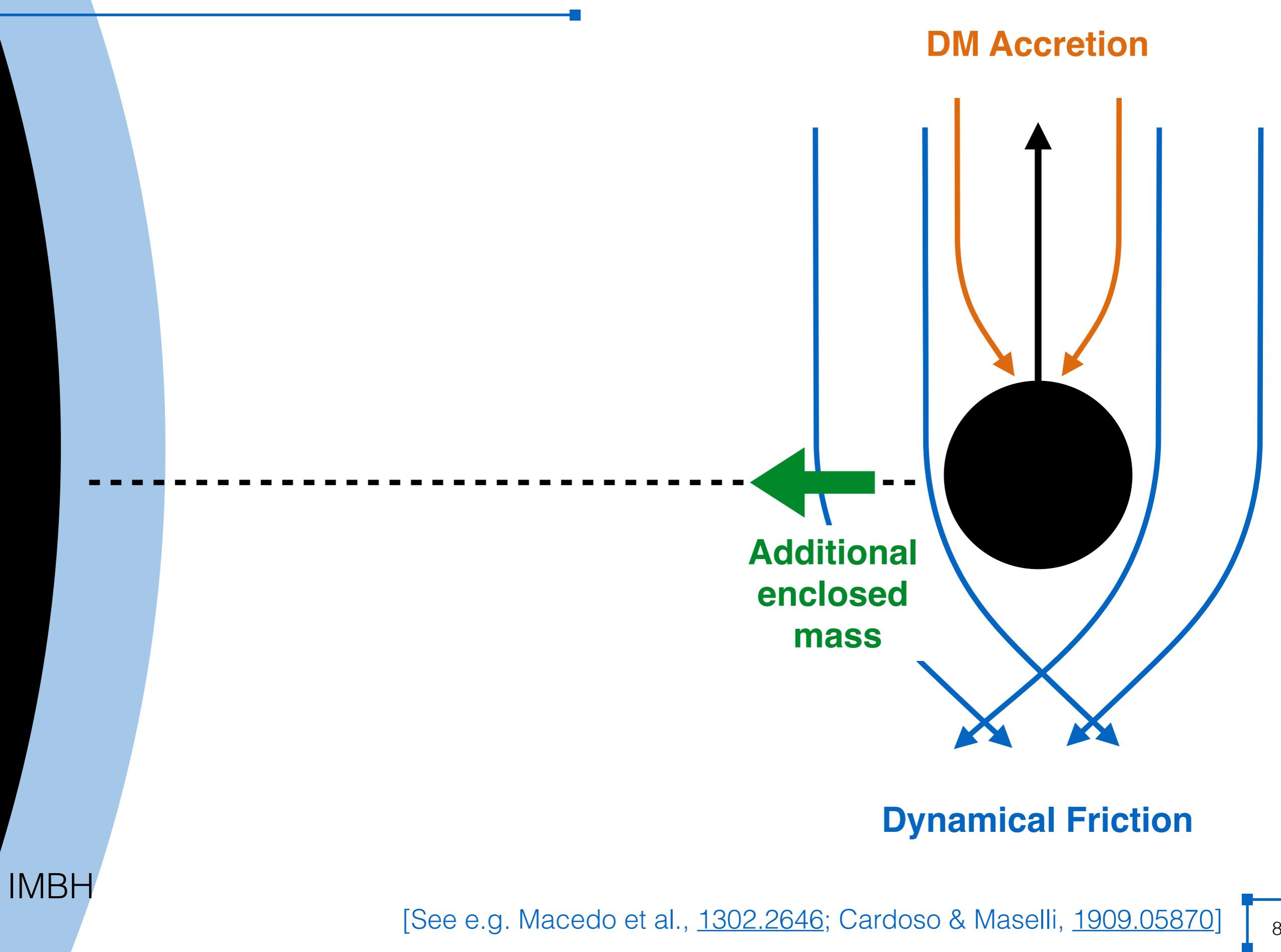


Red regions would be ruled out by observation of a DM spike!

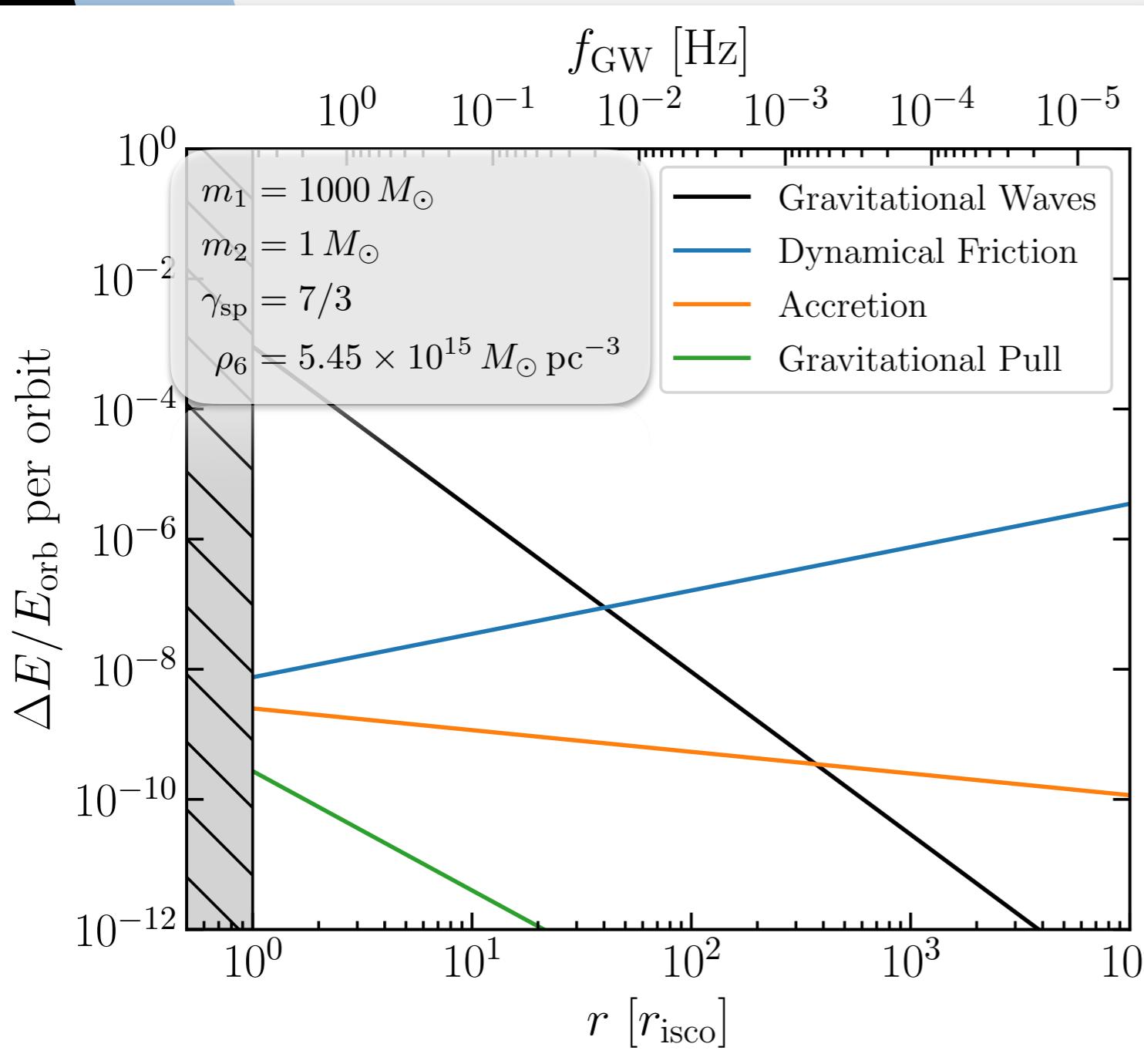
DM-induced Dephasing



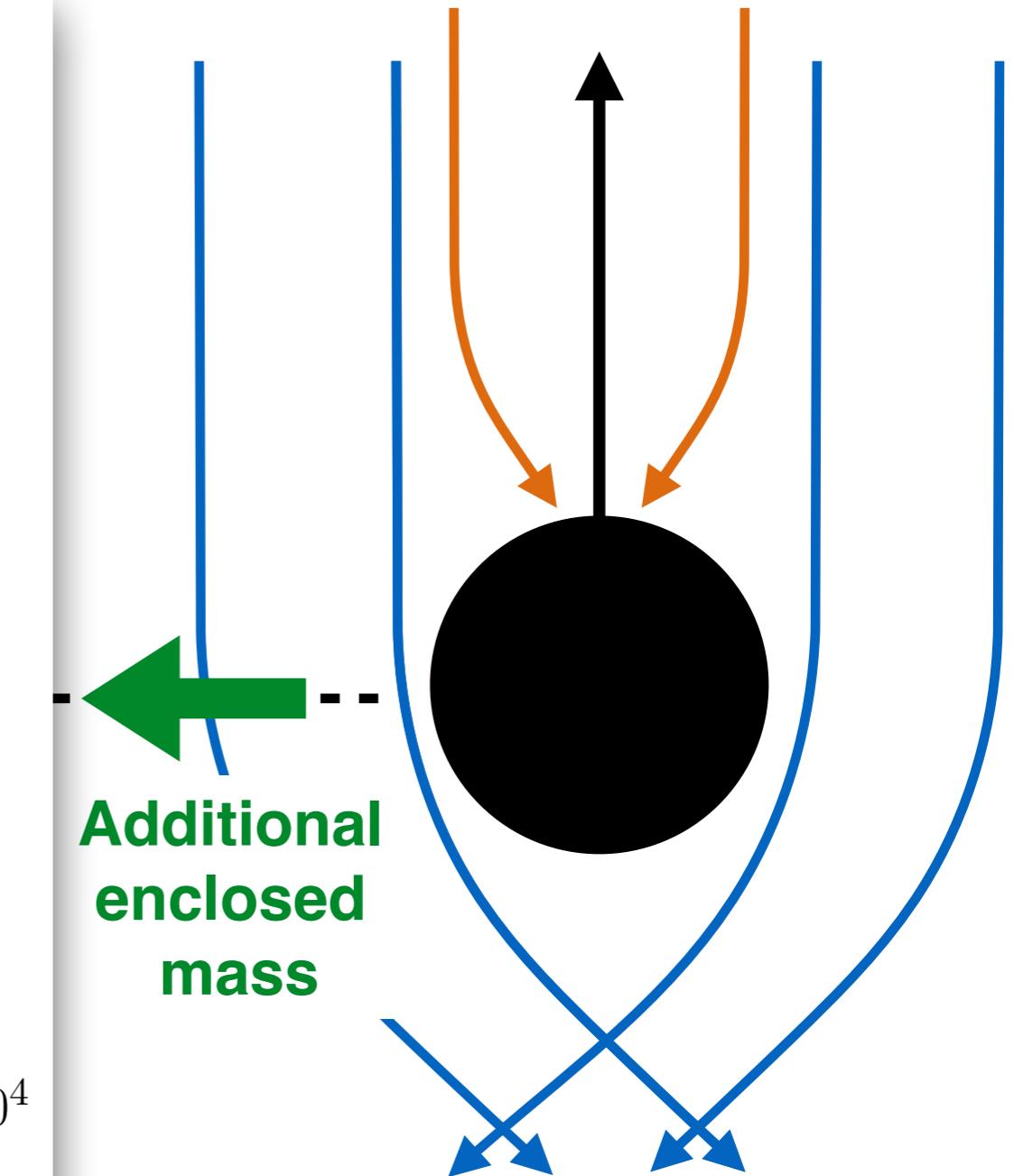
Impact of DM Spikes



Impact of DM Spikes



DM Accretion

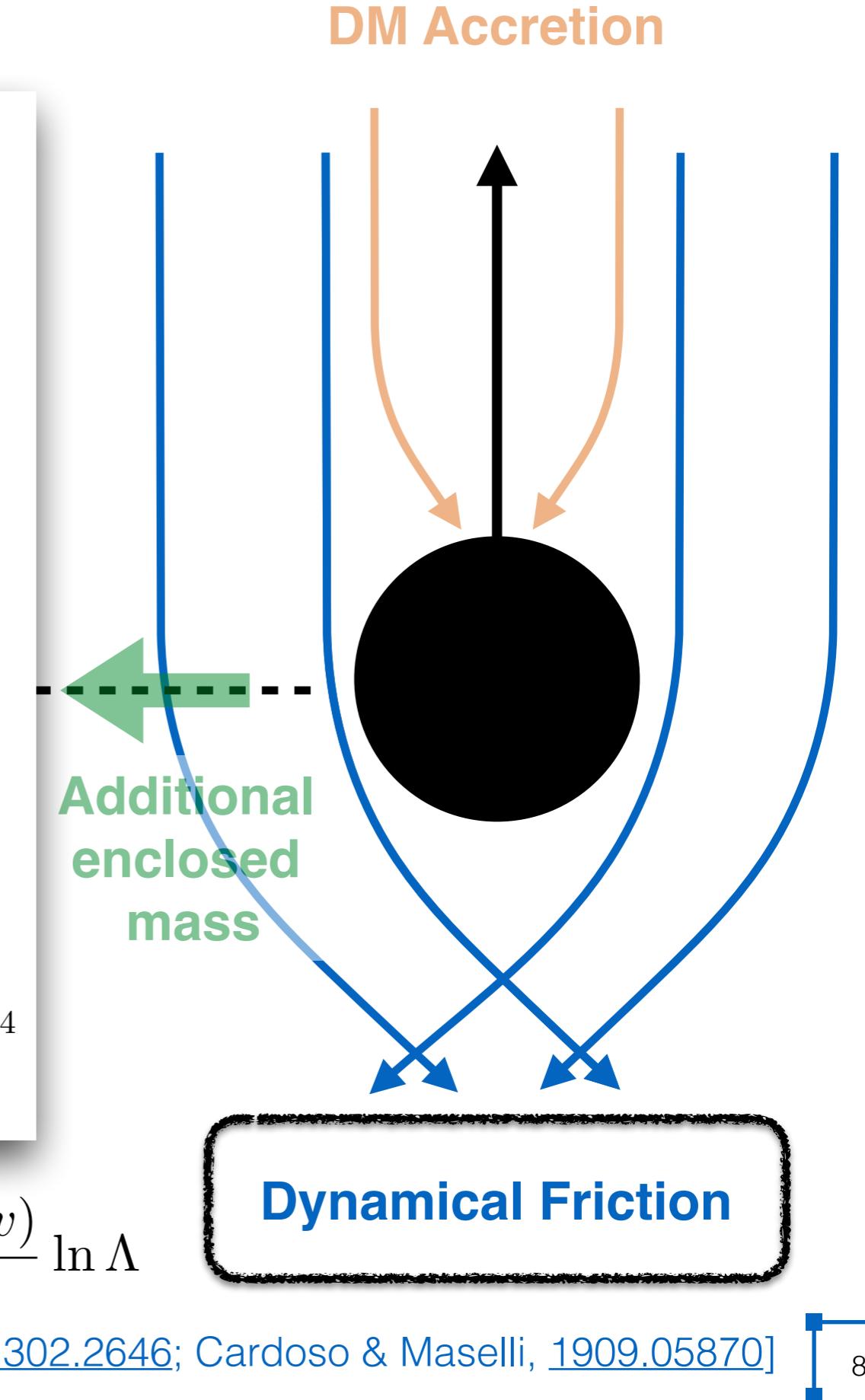
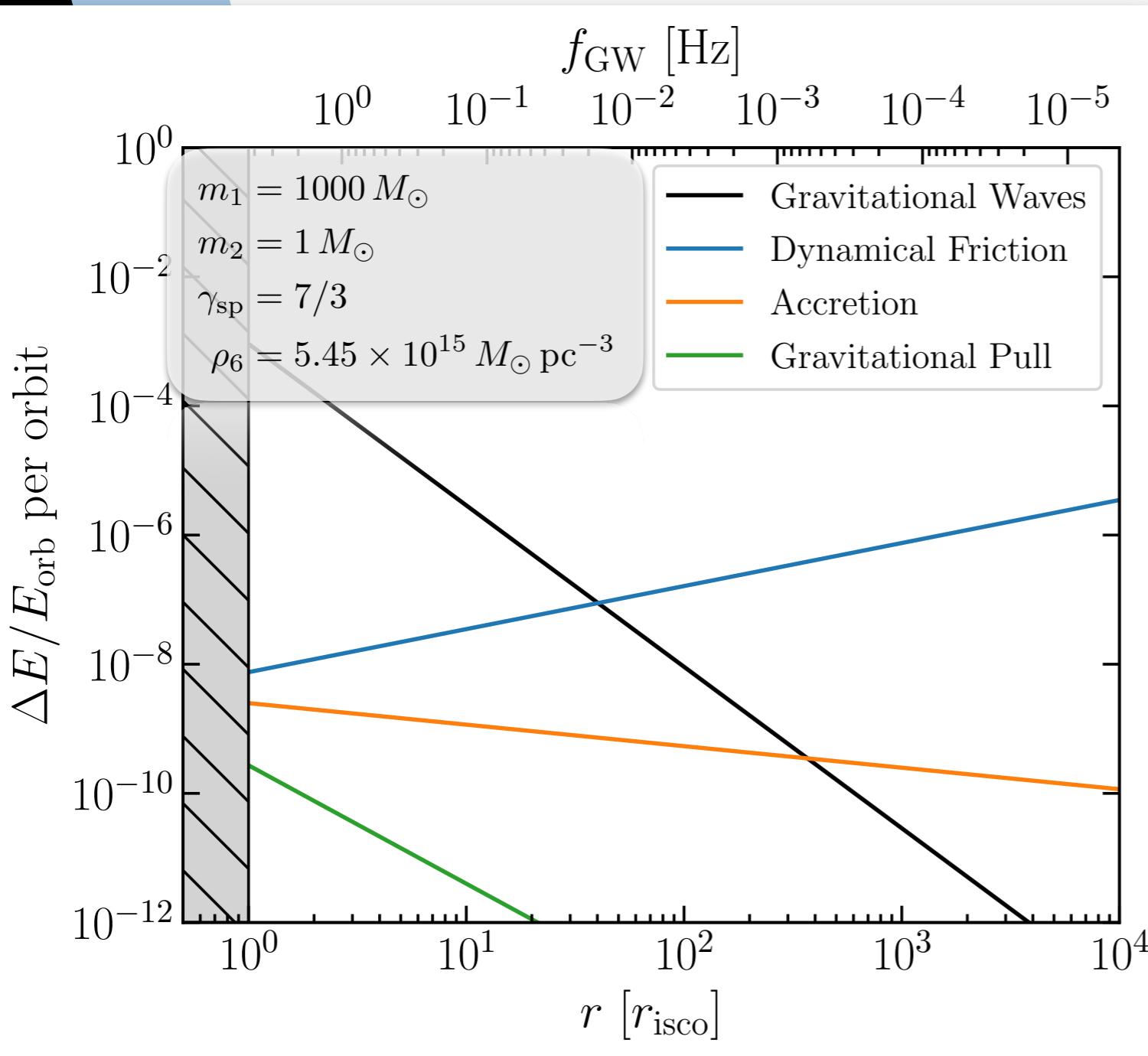


Dynamical Friction

IMBH

[See e.g. Macedo et al., [1302.2646](#); Cardoso & Maselli, [1909.05870](#)]

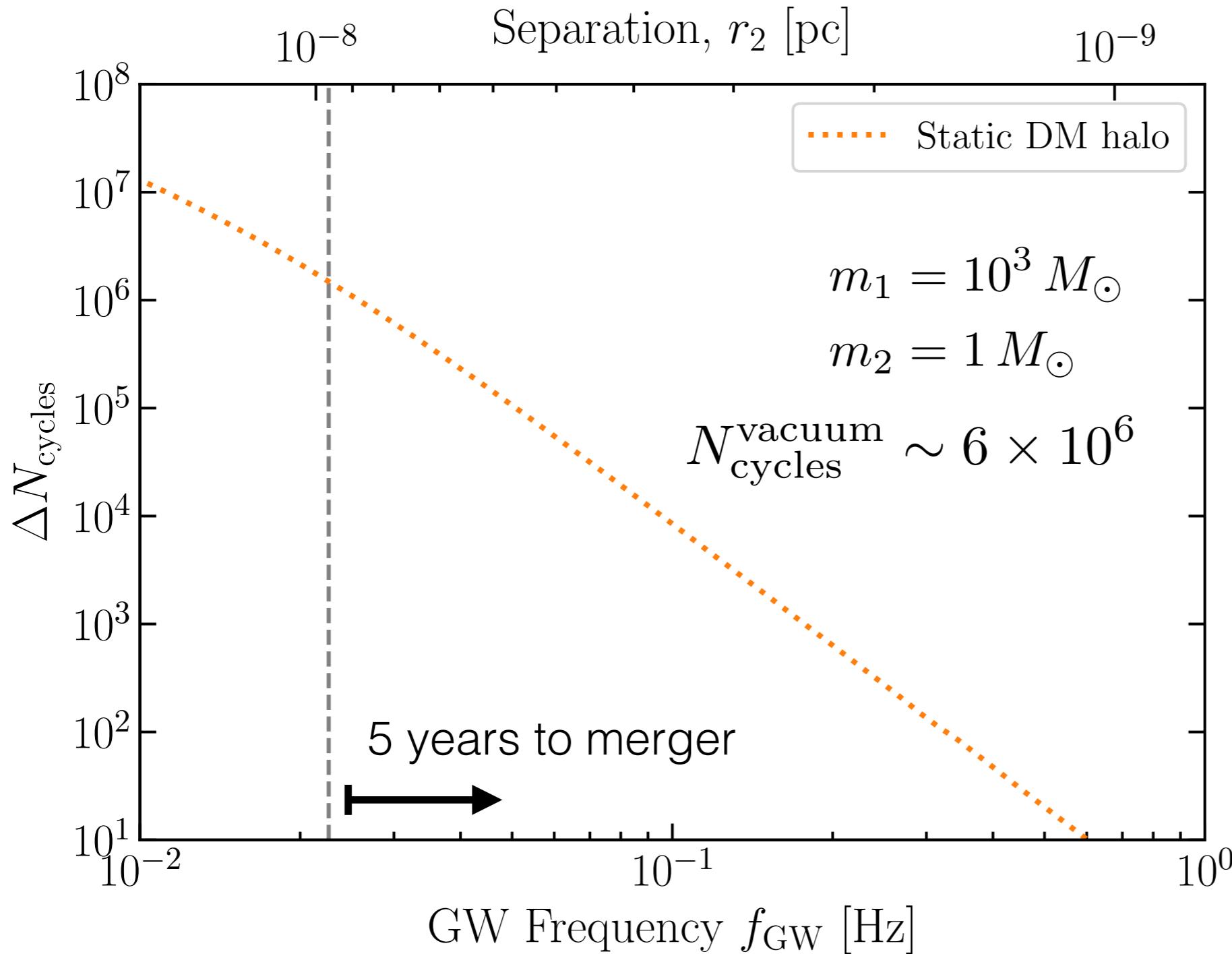
Impact of DM Spikes



$$\dot{E}_{\text{DF}} \sim \frac{4\pi G^2 m_2^2 \rho_{\text{DM}}(r) \xi(v)}{v} \ln \Lambda$$

[See e.g. Macedo et al., [1302.2646](#); Cardoso & Maselli, [1909.05870](#)]

Sizing up the dephasing



Assuming:

- quasi-circular orbits
 - Newtonian dynamics
 - Isotropic DM spike

$$m_1 = 10^3 M_\odot$$

$$m_2 = 1 M_\odot$$

$$N_{\text{cycles}}^{\text{vacuum}} \sim 6 \times 10^6$$

5 years to merger

$\Delta N_{\text{cycles}} \sim \mathcal{O}(10^6)$ cycles $\sim \mathcal{O}(1)$ effect

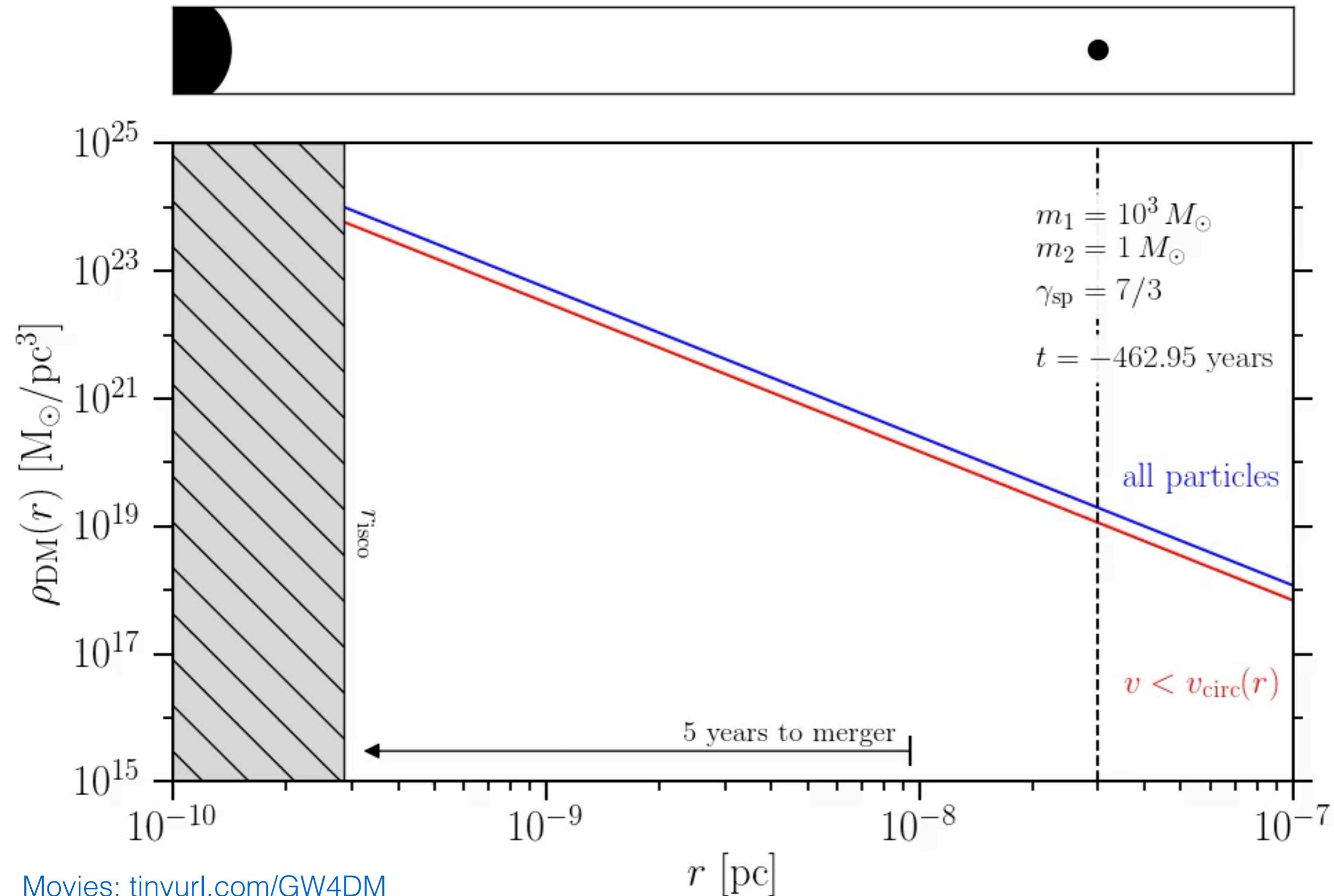
[Eda et al. 1301.5971, 1408.3534; see also 1302.2646, 1404.7140, 1404.7149 and others (sorry)]

Full evolution of the system

[BJK, Nichols, Gaggero & Bertone, 2002.12811]

Need to include **feedback** on the DM spike:

[Code available online:
github.com/bradkav/HaloFeedback]

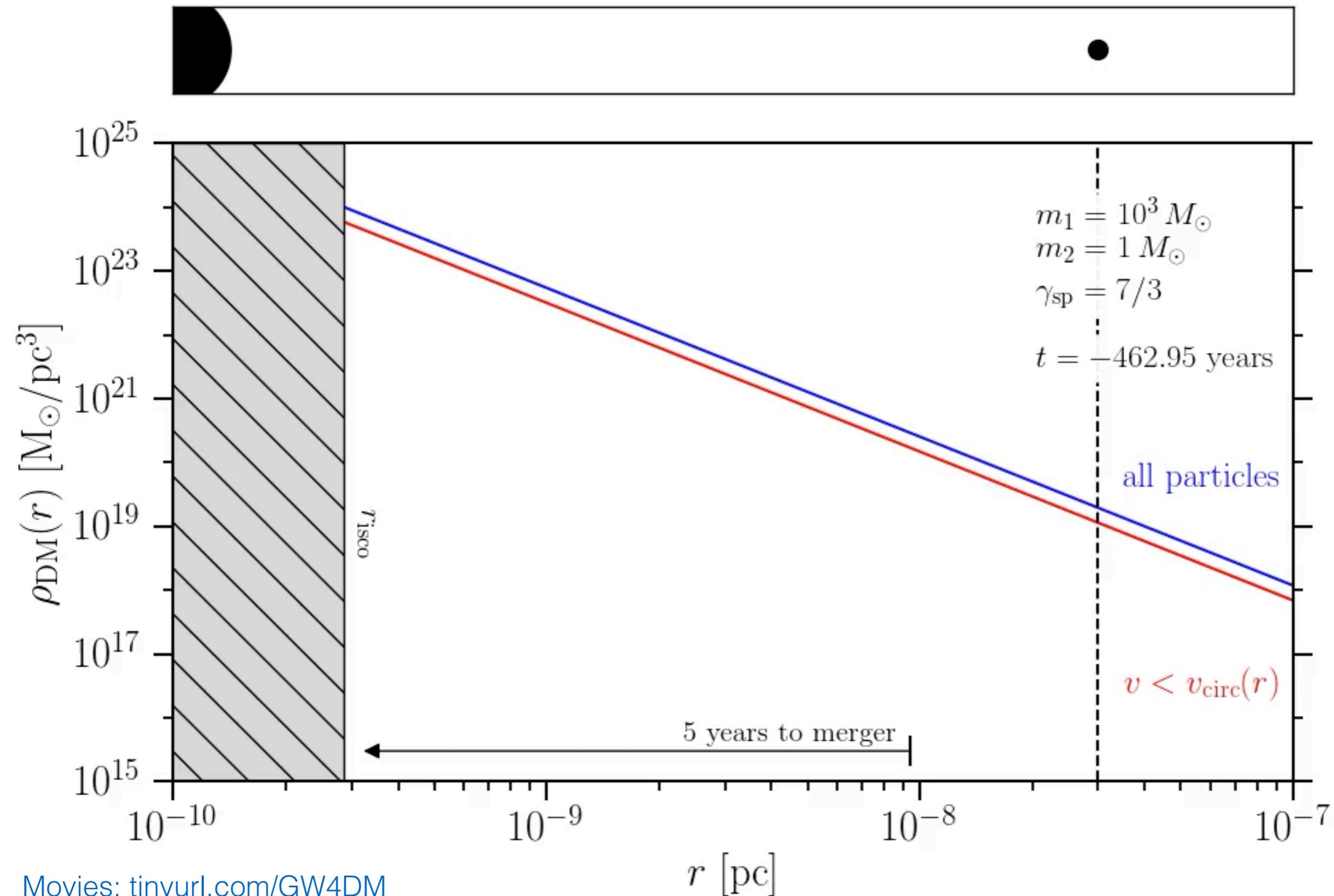


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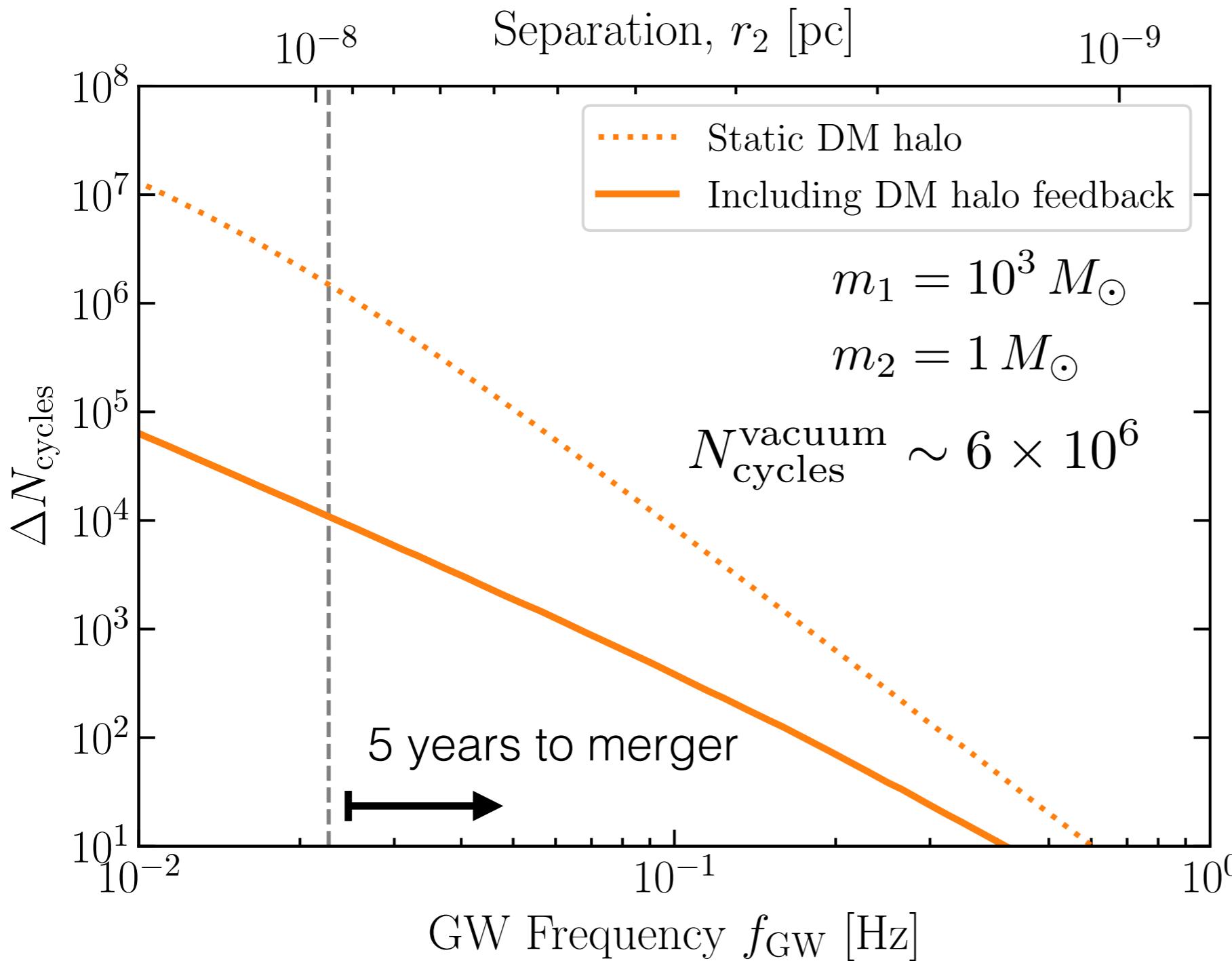
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Sizing up the dephasing

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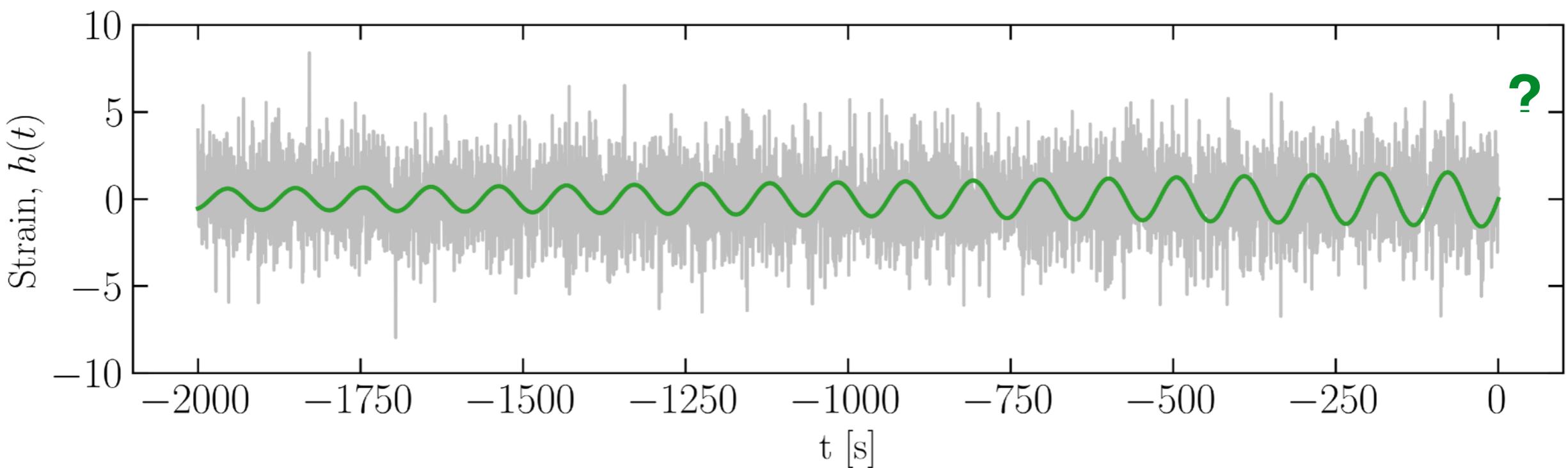
Assuming:

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- Newtonian dynamics
- Isotropic DM spike

Feedback effect becomes smaller as q decreases, but so does the size of the dephasing effect...

$$\Delta N_{\text{cycles}} \sim \mathcal{O}(10^4) \text{ cycles} \sim \% \text{ level effect}$$

A more realistic scenario



Want to address questions of:

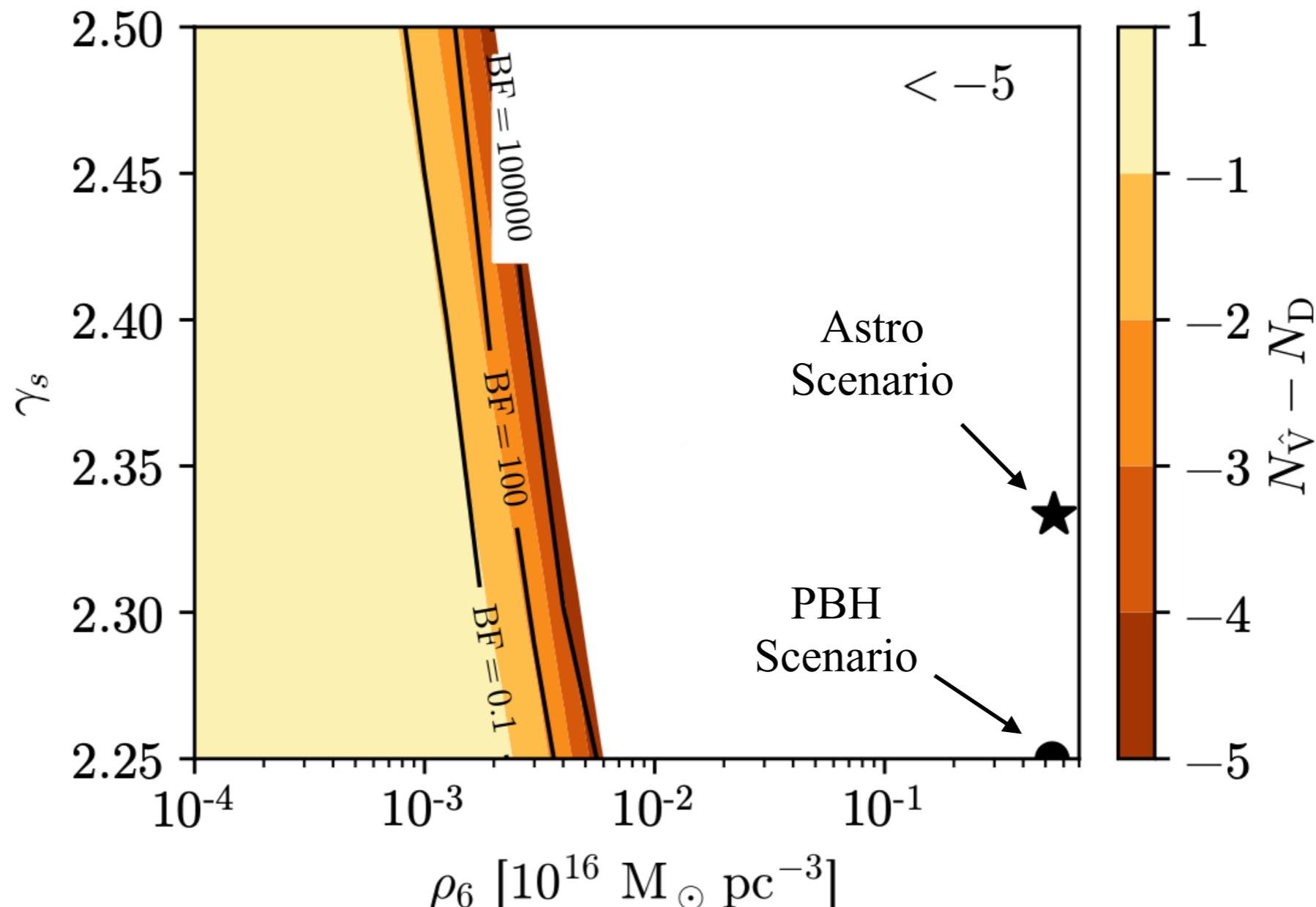
- **Discoverability** - can we tell it apart from a *GR-in-vacuum* waveform?
- **Measurability** - can we pin down the properties of the system (*especially the DM*)?

Discoverability

[Code available online:
<https://github.com/adam-coogan/pydd>]

$$q = m_2/m_1$$

We'll call a DM spike **discoverable** if it can be distinguished from a GR-in-vacuum system.

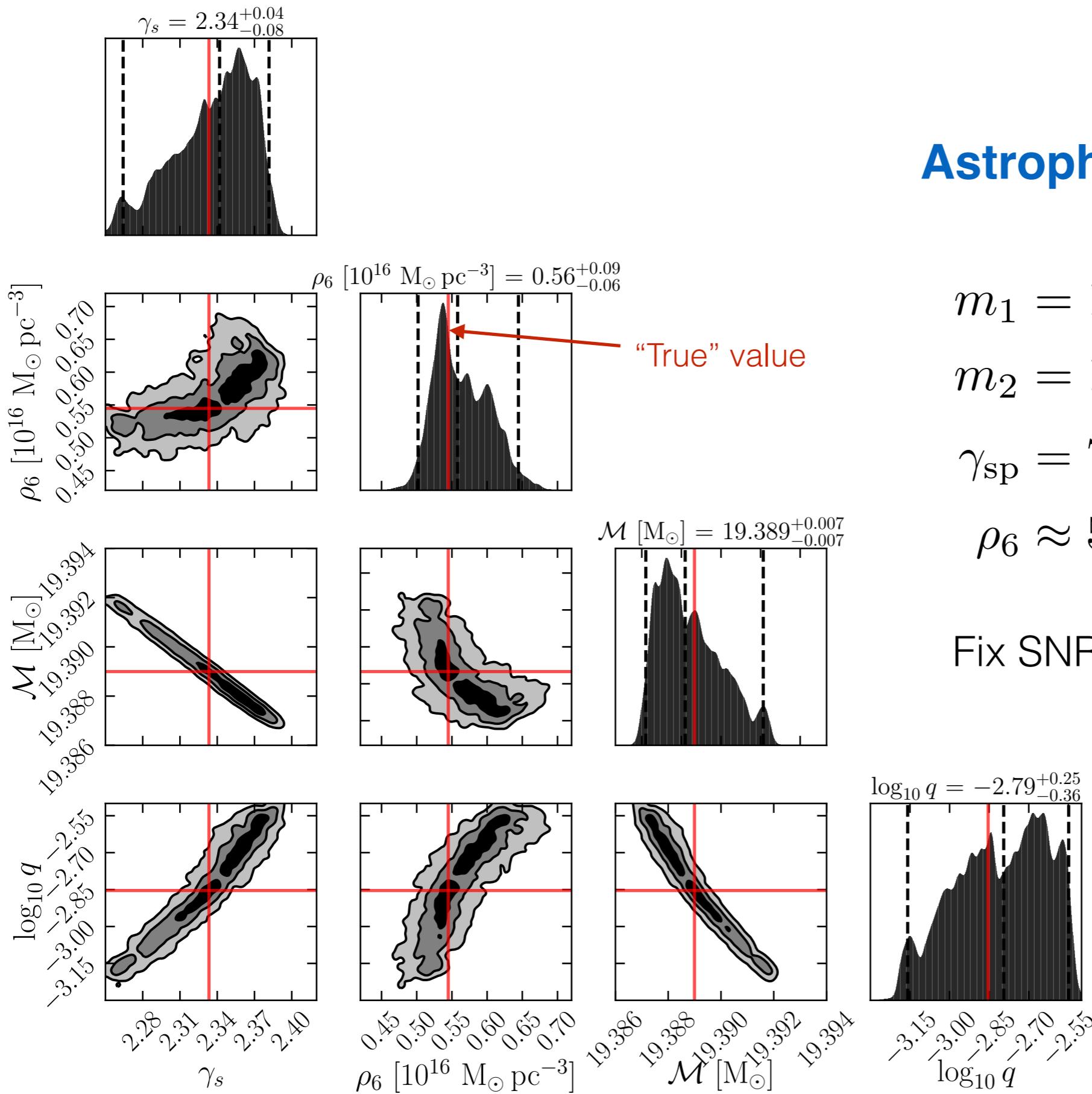


Compute Bayes Factor (BF) comparing Bayesian evidence for **Vacuum** and **Dressed** systems, with parameters:

vs.

Measurability

[Coogan, Bertone, Gaggero, **BJK** & Nichols, [2108.04154](#)]



Astrophysical scenario

$$m_1 = 10^3 M_\odot$$

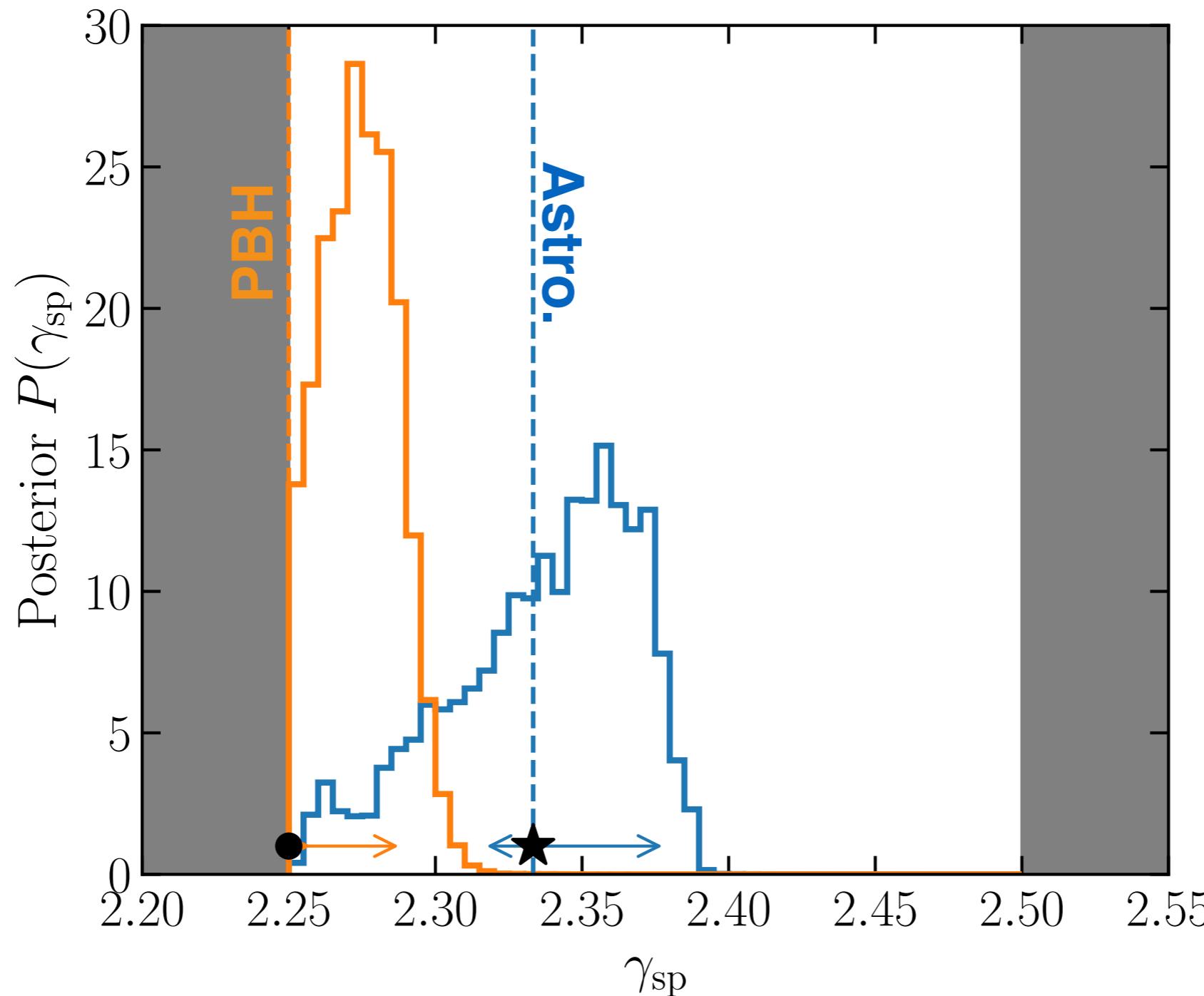
$$m_2 = 1 M_\odot$$

$$\gamma_{\text{sp}} = 7/3 \approx 2.3333\dots$$

$$\rho_6 \approx 5.45 \times 10^{15} M_\odot \text{ pc}^{-3}$$

Measurability - Spike Shape

[Coogan, Bertone, Gaggero, **BJK** & Nichols, [2108.04154](#)]



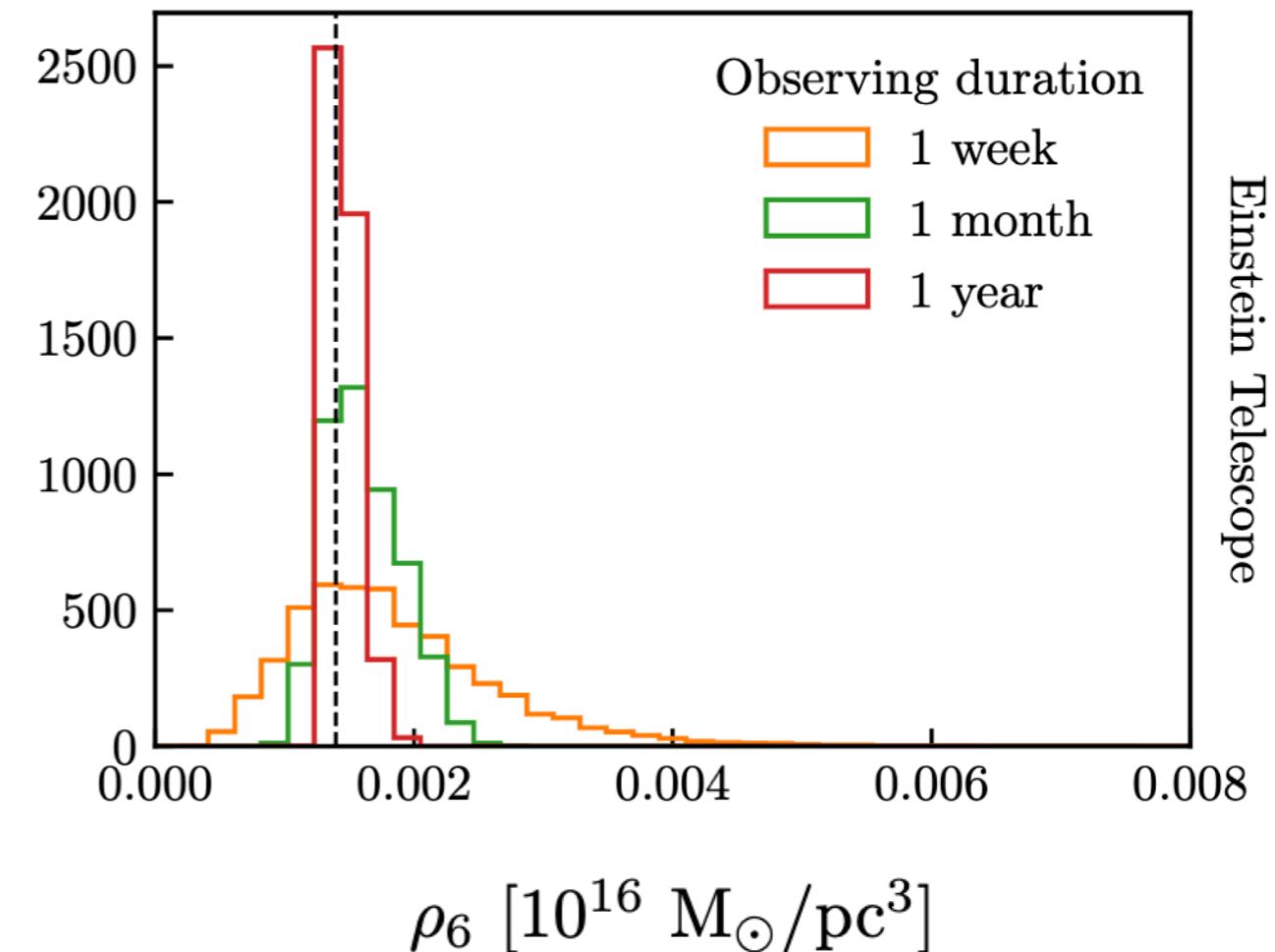
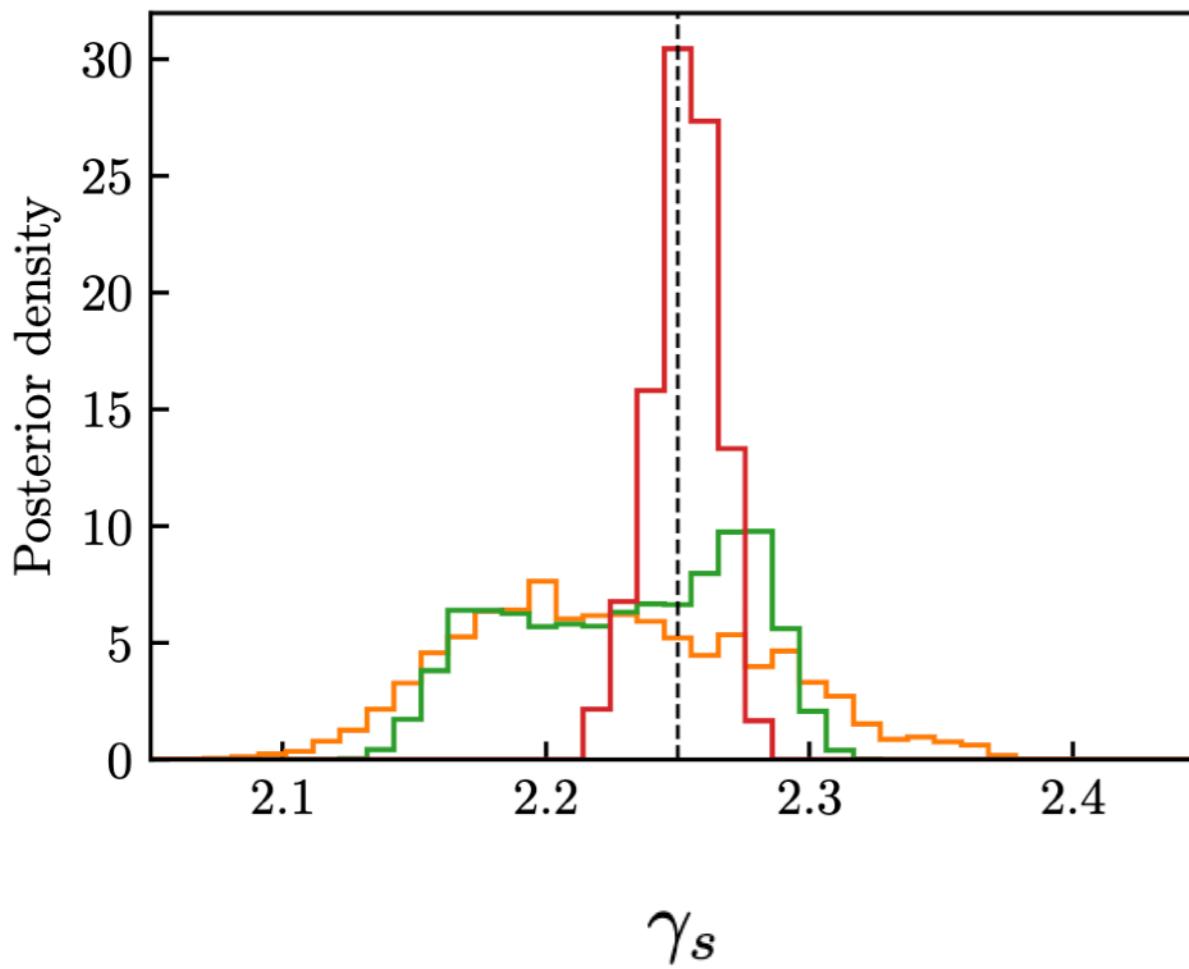
We may be able to distinguish different *shapes* of spike
→ Different DM models and formation mechanisms!

Light PBH Binaries

[Bertone, Cole, Coogan & **BJK**, in preparation]

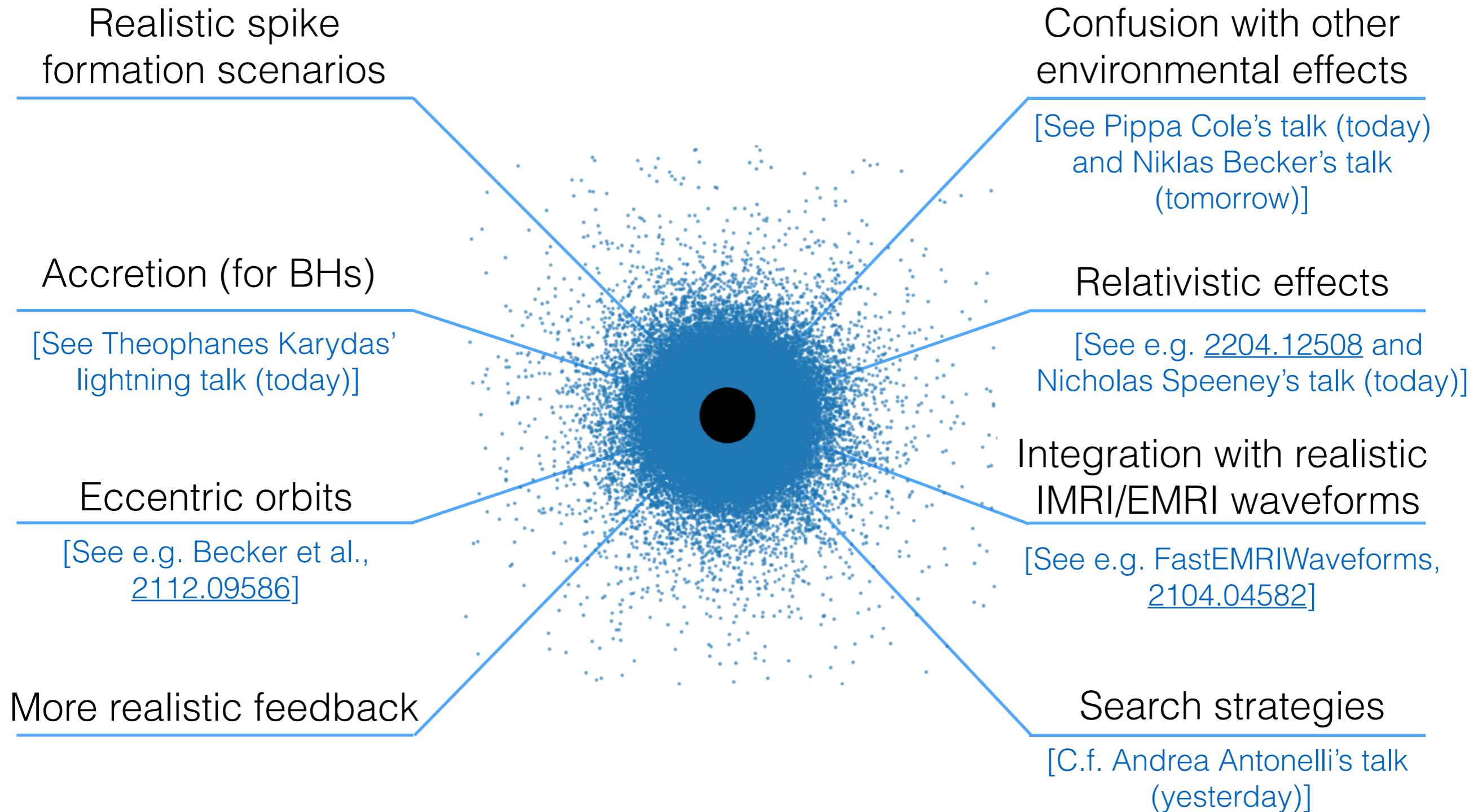
Ground-based telescopes (Einstein Telescope, Cosmic Explorer, perhaps even LVK) could also measure DM spikes in **lighter binaries** (in this case PBHs):

$$(m_1, m_2) = (1, 10^{-3}) M_{\odot}$$

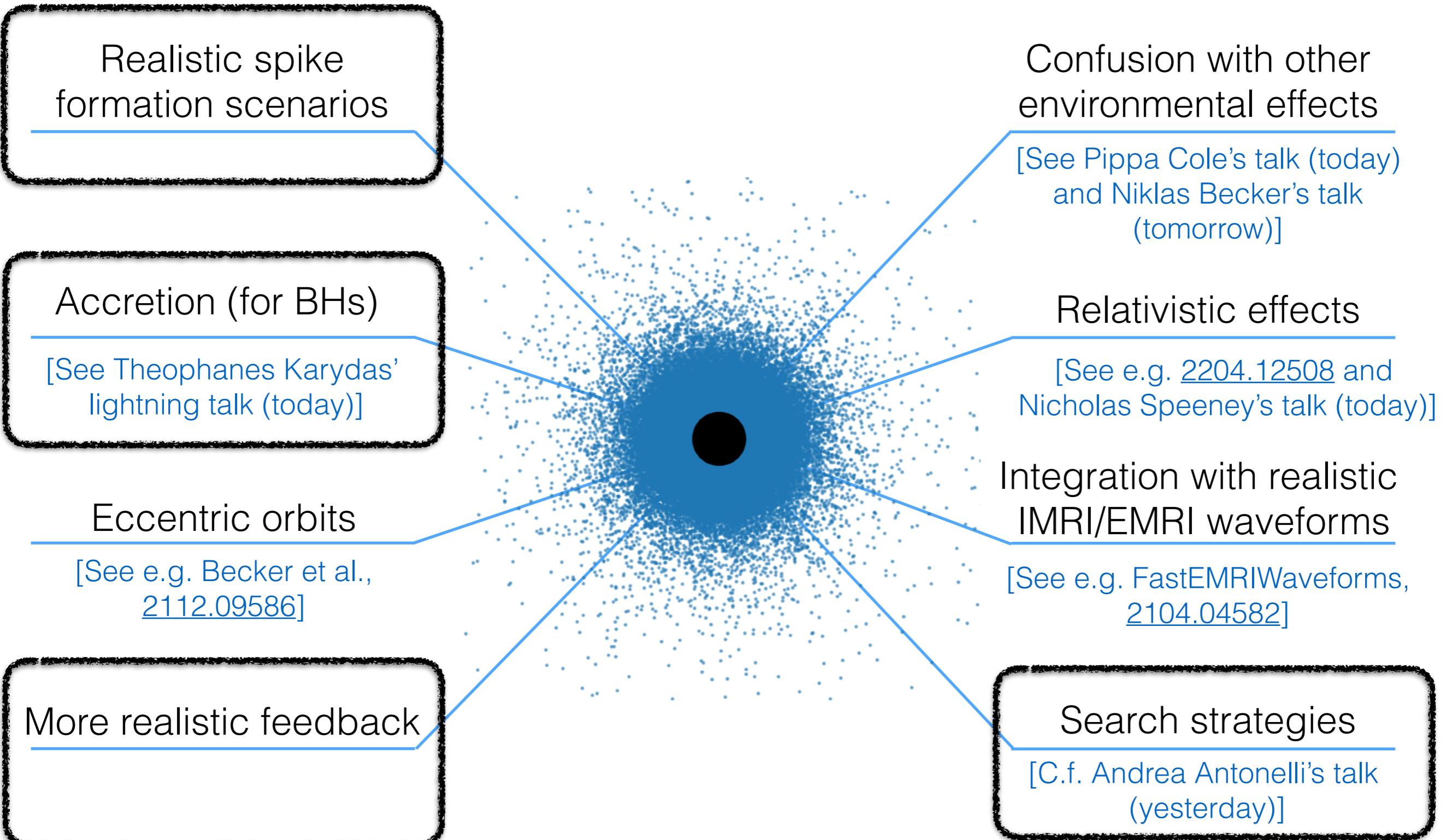


Detectable out to ~ 100 Mpc, with the ‘dressed’ system massively favoured, even with ‘short’ observations (~ 1 week)

Towards better spikes

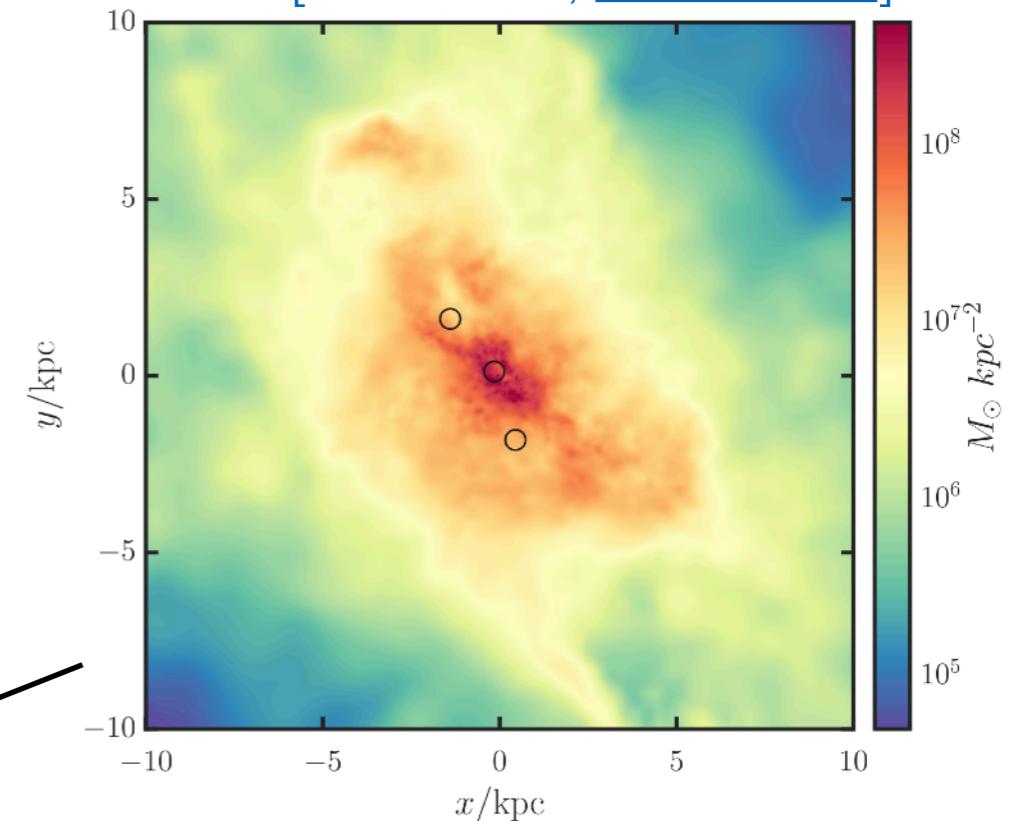
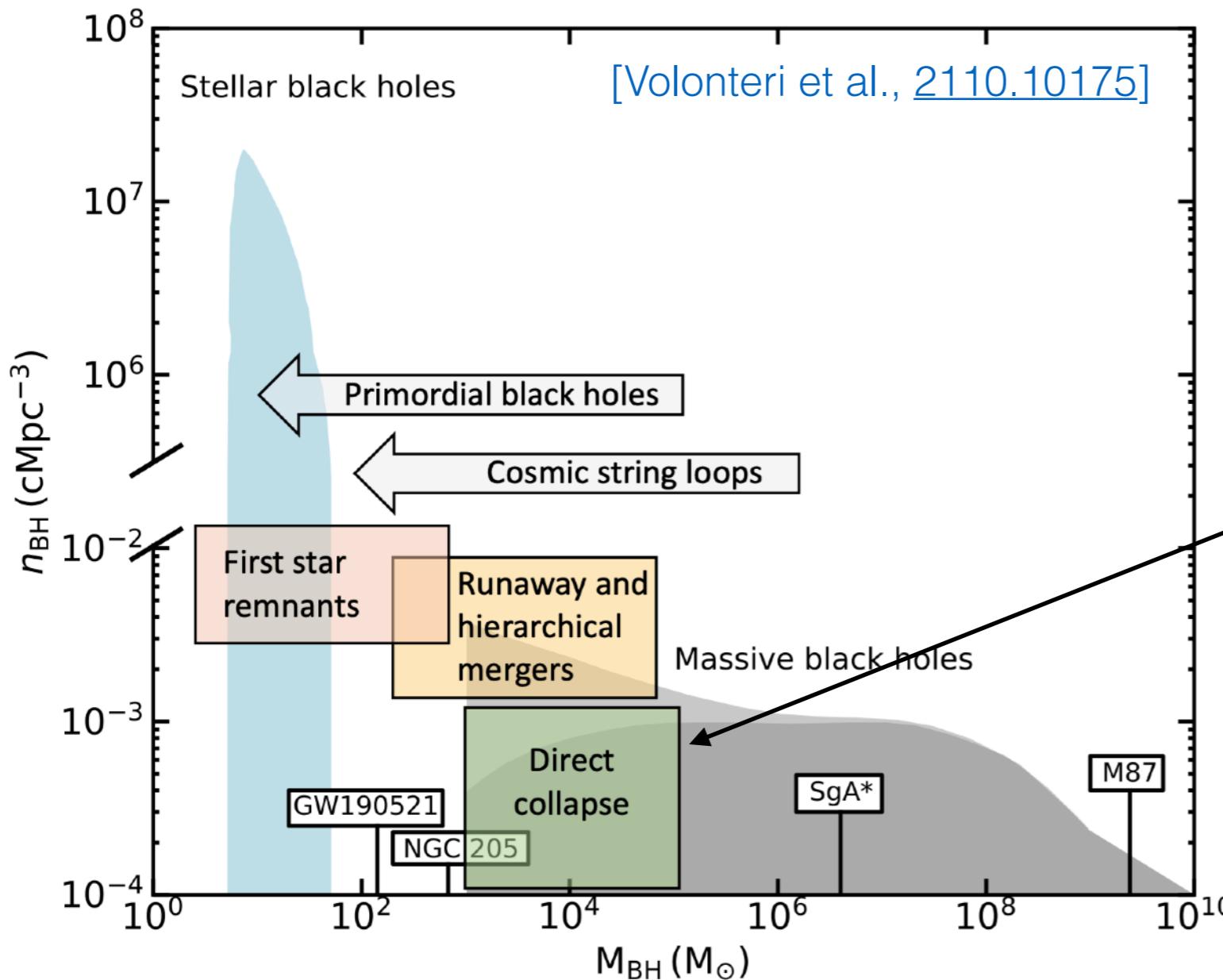


Towards better spikes



Black Hole and Spike Formation

[Dunn et al., 1803.01007]

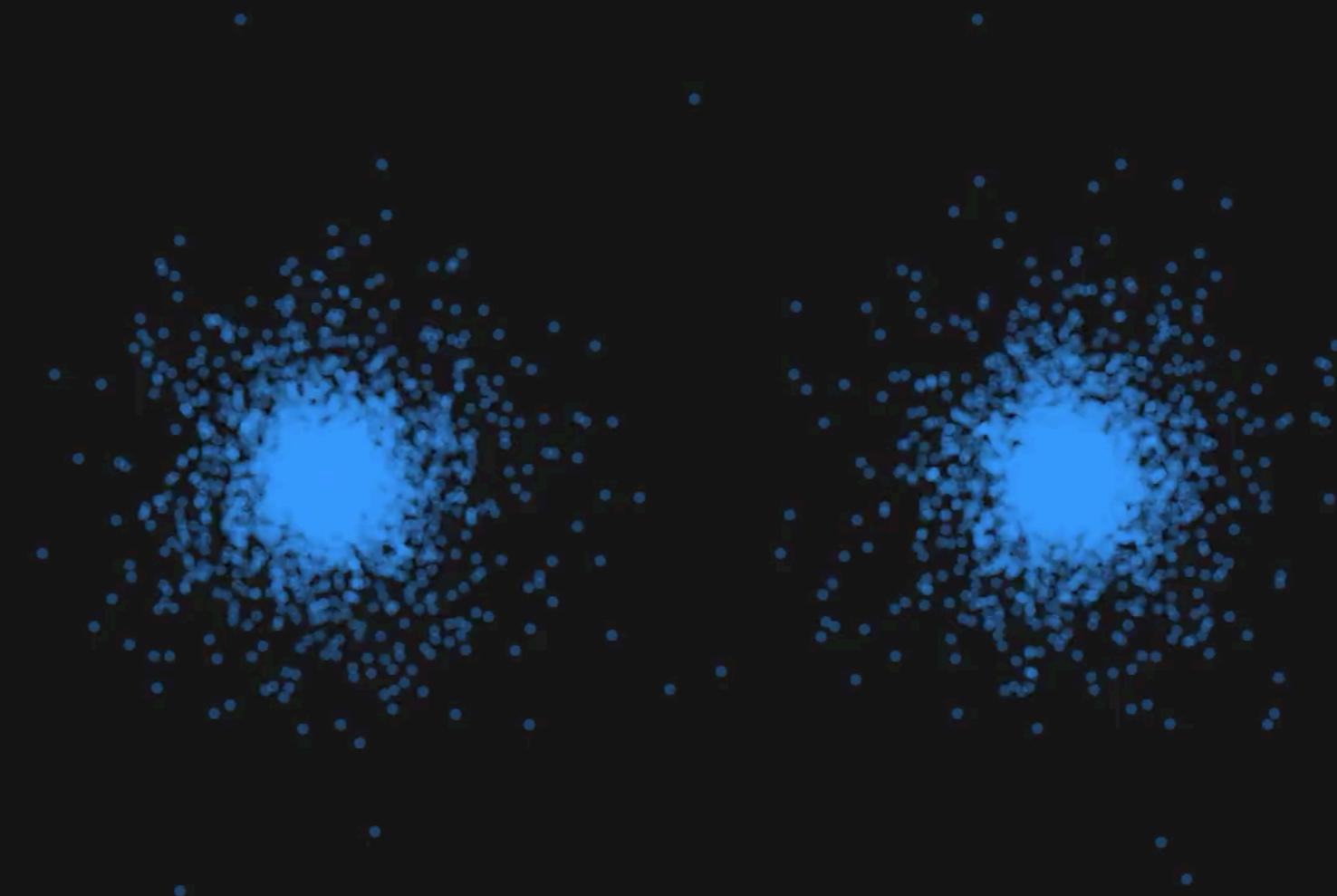


Use semi-analytic galaxy formation models to study the properties of Direct Collapse Black Holes and the halos they form in.

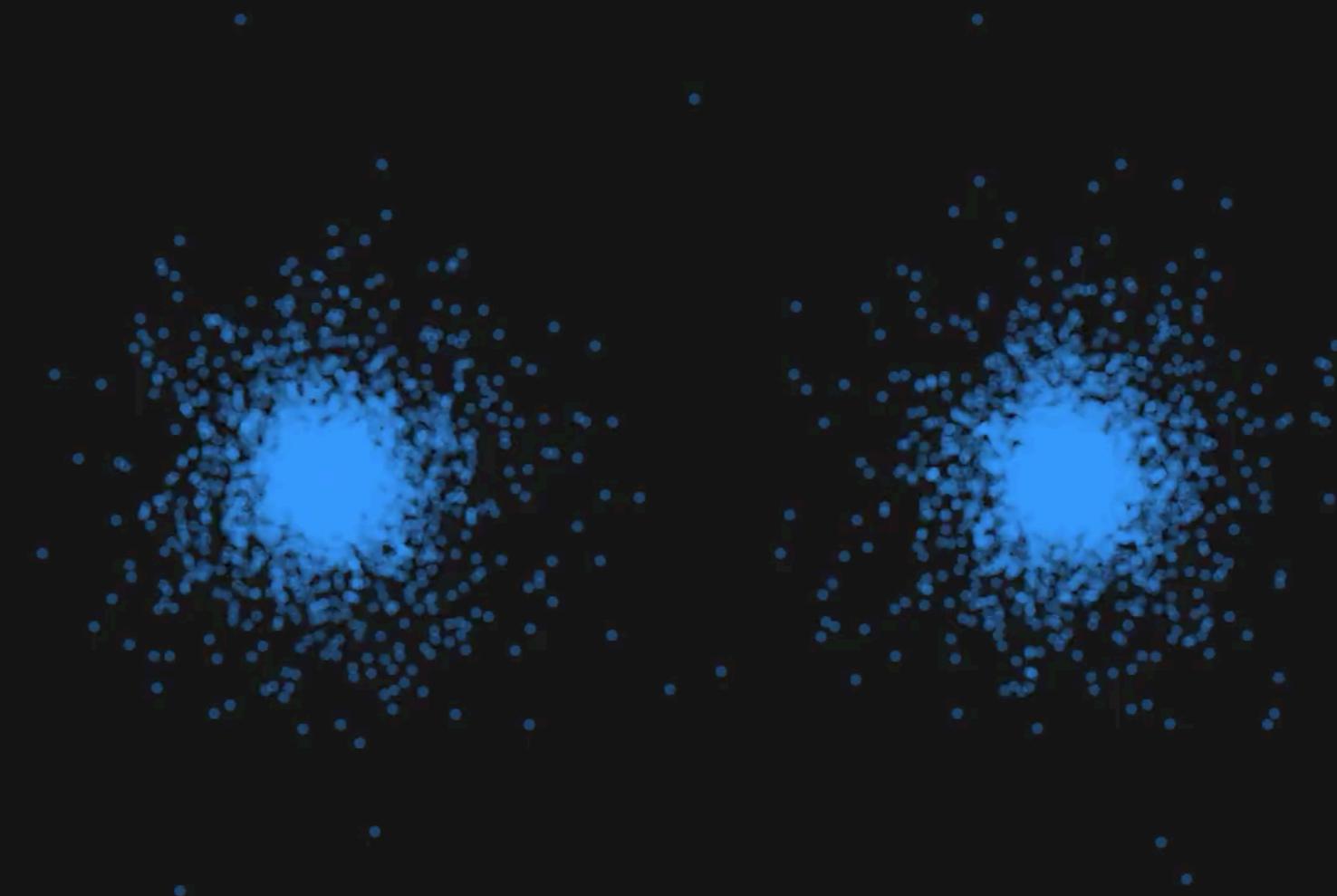
Preliminary results suggest that large densities are possible $\rho_6 \gtrsim 10^{16} M_{\odot} \text{ pc}^{-3}$ but do these systems survive, and are they common?

[Work in progress with Abram Perez, Pratika Dayal, and others]

- $M_{\text{PBH}} = 30 M_{\odot}$; $a_i = 0.01 \text{ pc}$; $e_i = 0.995$
 $T = 0.00 \text{ kyr}$

 10^{-2} pc

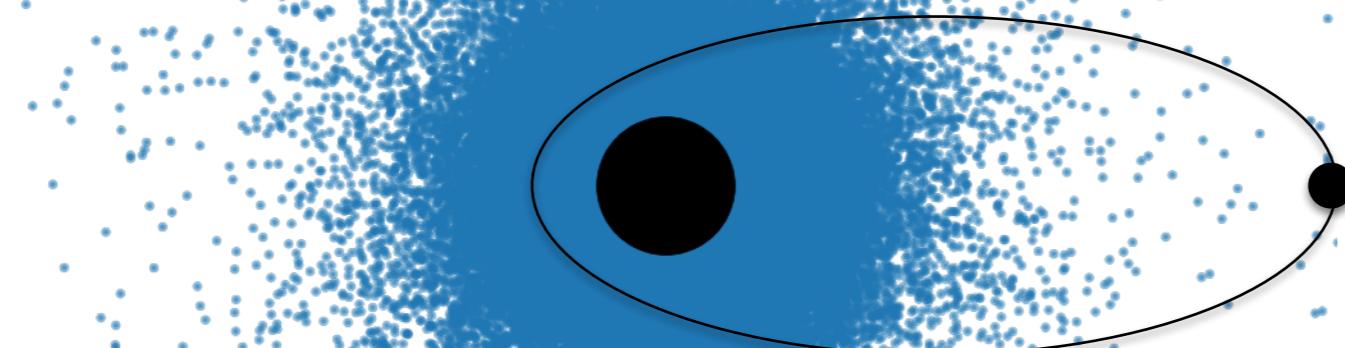
- $M_{\text{PBH}} = 30 M_{\odot}$; $a_i = 0.01 \text{ pc}$; $e_i = 0.995$
 $T = 0.00 \text{ kyr}$

 10^{-2} pc

Dressed PBH IMRIs

PBH binaries typically formed (in the early Universe) with very high eccentricity —> Rapid merger

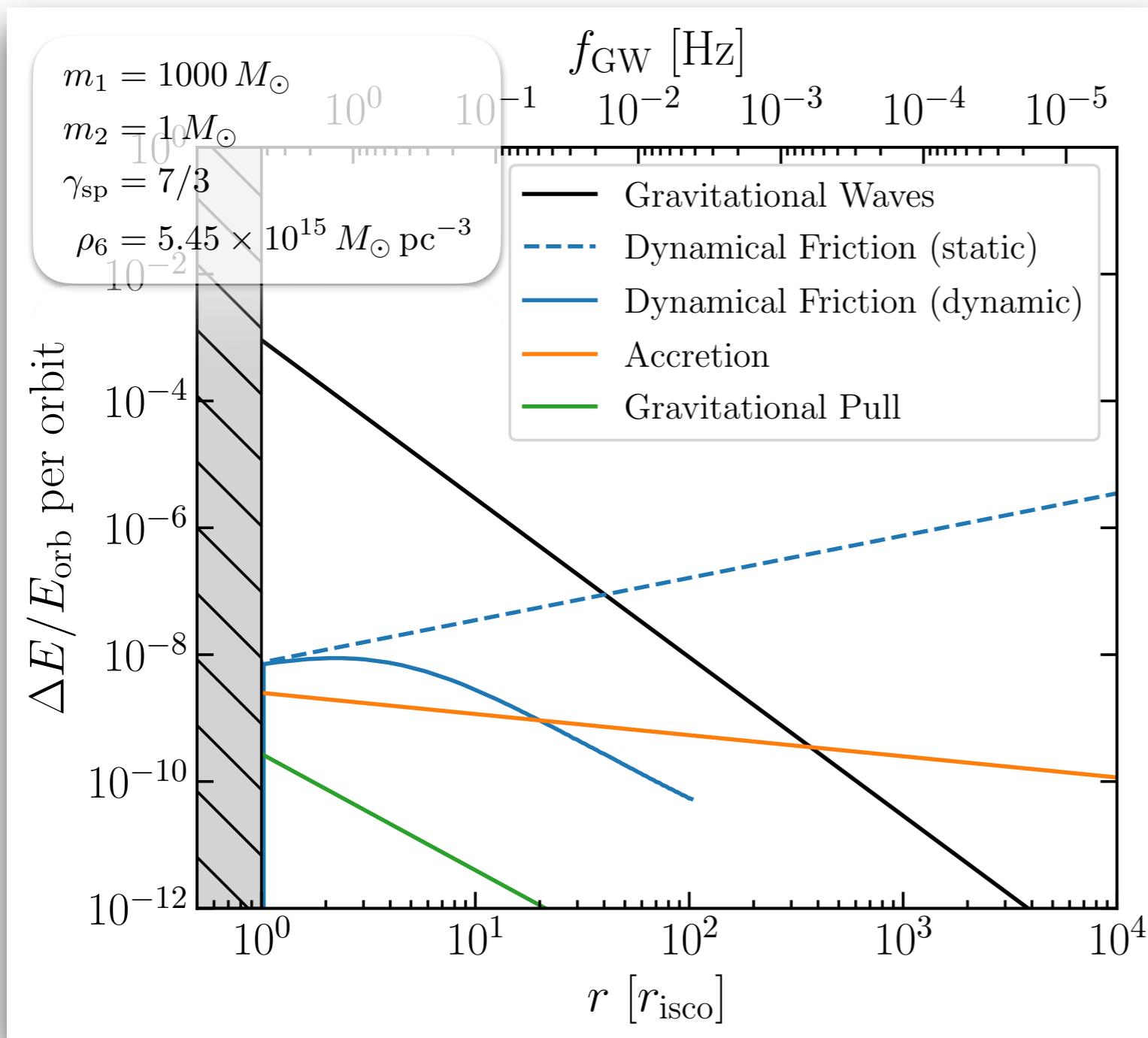
$$t_{\text{merge}} \sim a_i^4 (1 - e_i^2)^{7/2}$$



Dark Dresses around PBH IMRIs are likely to accelerate merger...

Do dressed PBH IMRIs merge slowly enough to be detected at low redshift?

Accretion (and other effects)



More realistic feedback

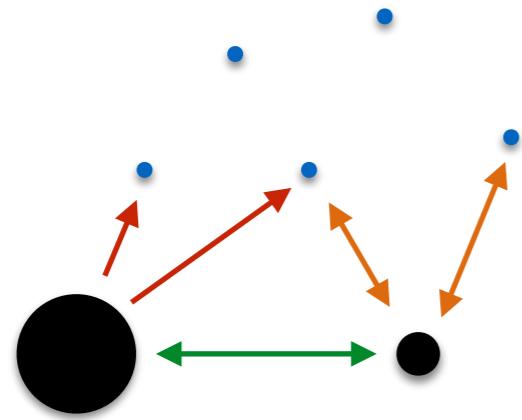
Eventually need to expand our description of feedback in the DM spike:

- Anisotropy in the DM distribution
- Multiple sources of feedback (dynamical friction, accretion, etc)
- Verify semi-analytic prescriptions

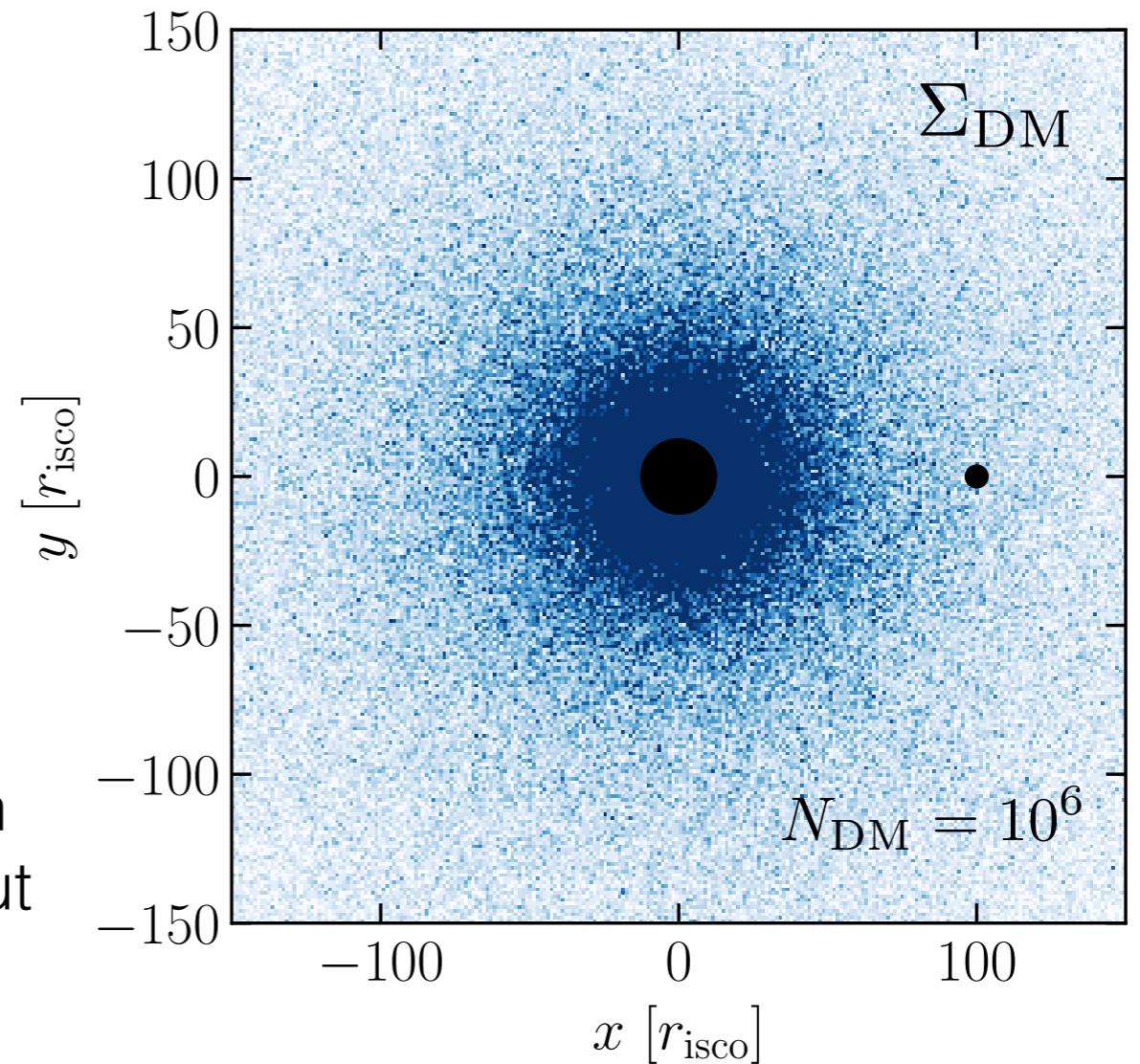
NbodyIMRI: solver tailored to DM spikes

[Code here: github.com/bradkav/NbodyIMRI]

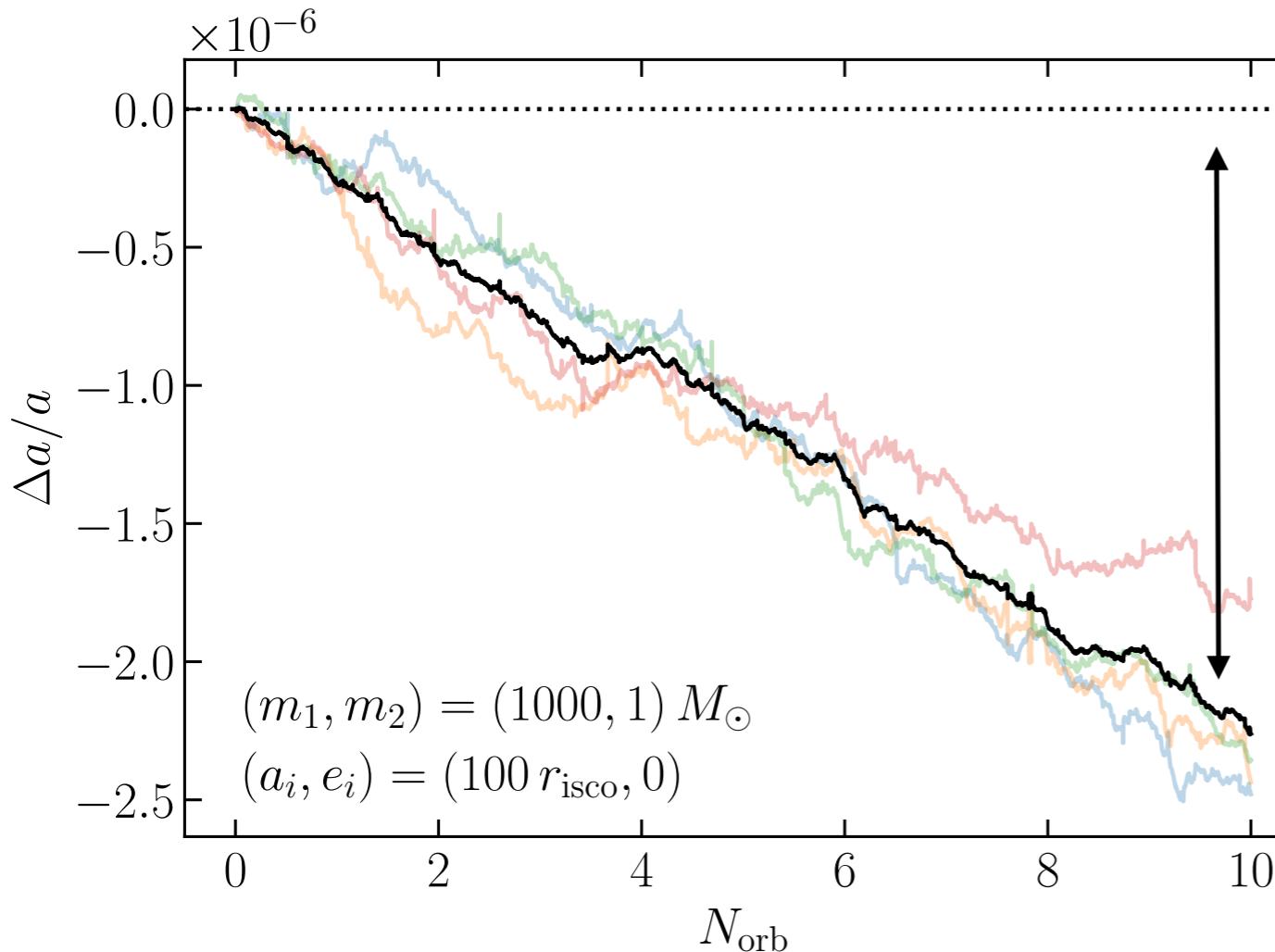
No *DM-DM* interparticle forces



Can follow the spike in high resolution
(For now in Newtonian gravity only, but eventually include PN corrections)



More realistic feedback



Rate of energy loss allows us to calibrate dynamical friction force

Which particles are scattered by the secondary?

How much of the spike is depleted?

N-body simulations will never be fast enough to generate waveforms, but they help inform and calibrate modelling.

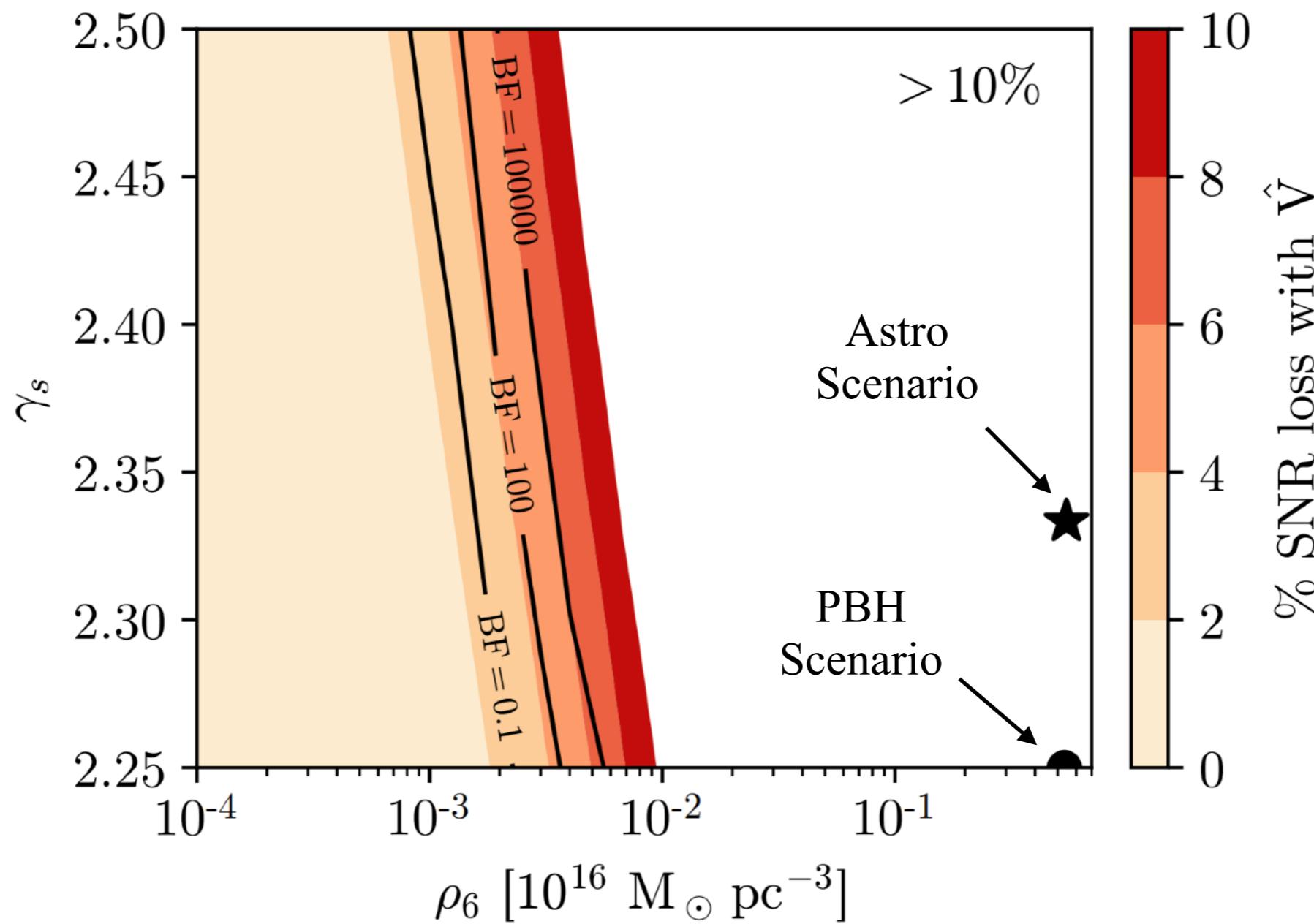
Ultimately need a fast method of generating waveforms (e.g. surrogate models?).

But even if we can eventually model the system perfectly (and quickly), we still have a challenge...

Discoverability

[Code available online:
<https://github.com/adam-coogan/pydd>]

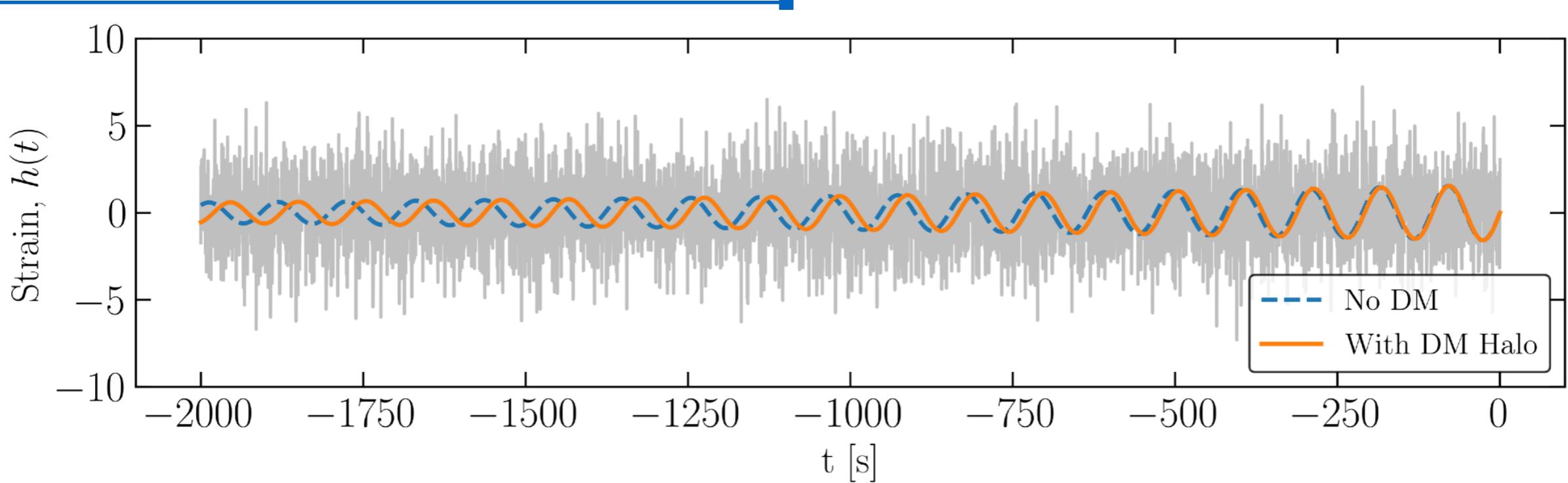
Substantial **loss of SNR** using GR-in-vacuum waveforms!



Space of templates would need to be expanded *a lot*
(with possible complicated correlations...)

[See e.g. Alvin Chua's talk (yesterday)]

Search strategies?

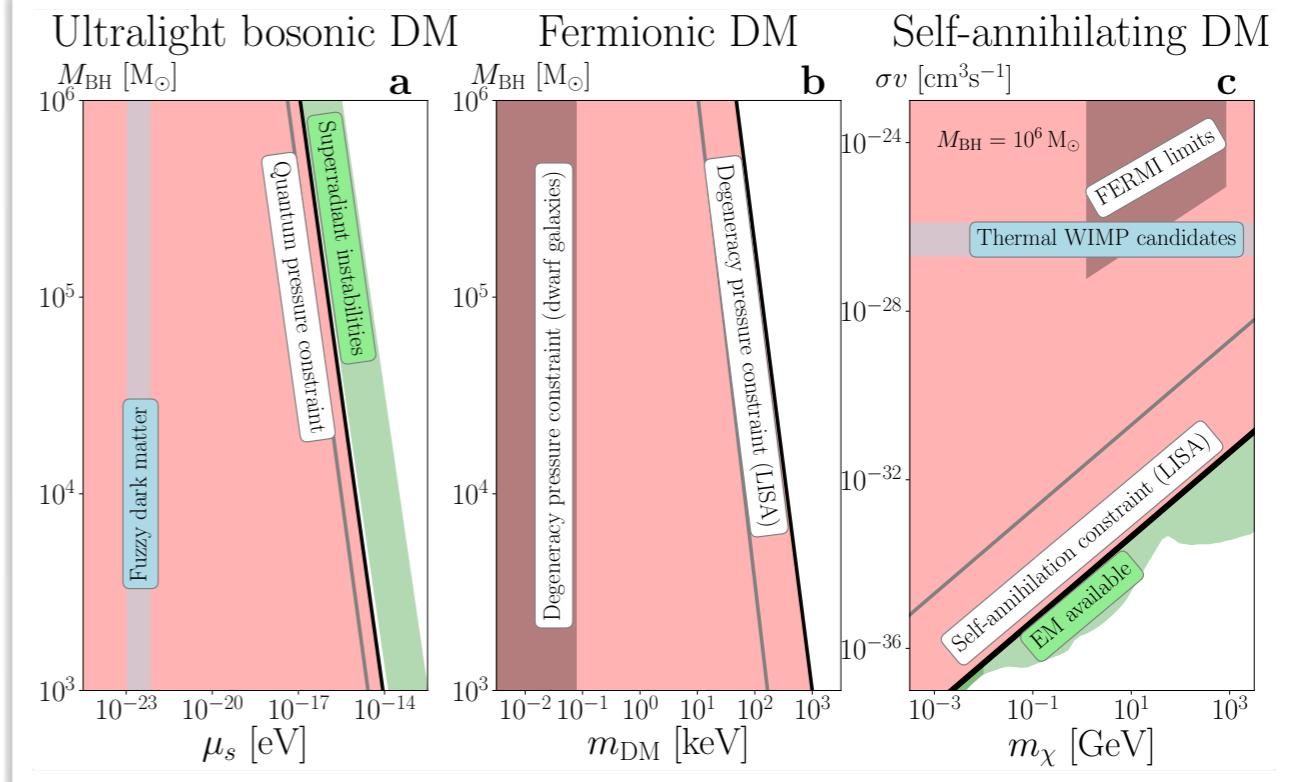
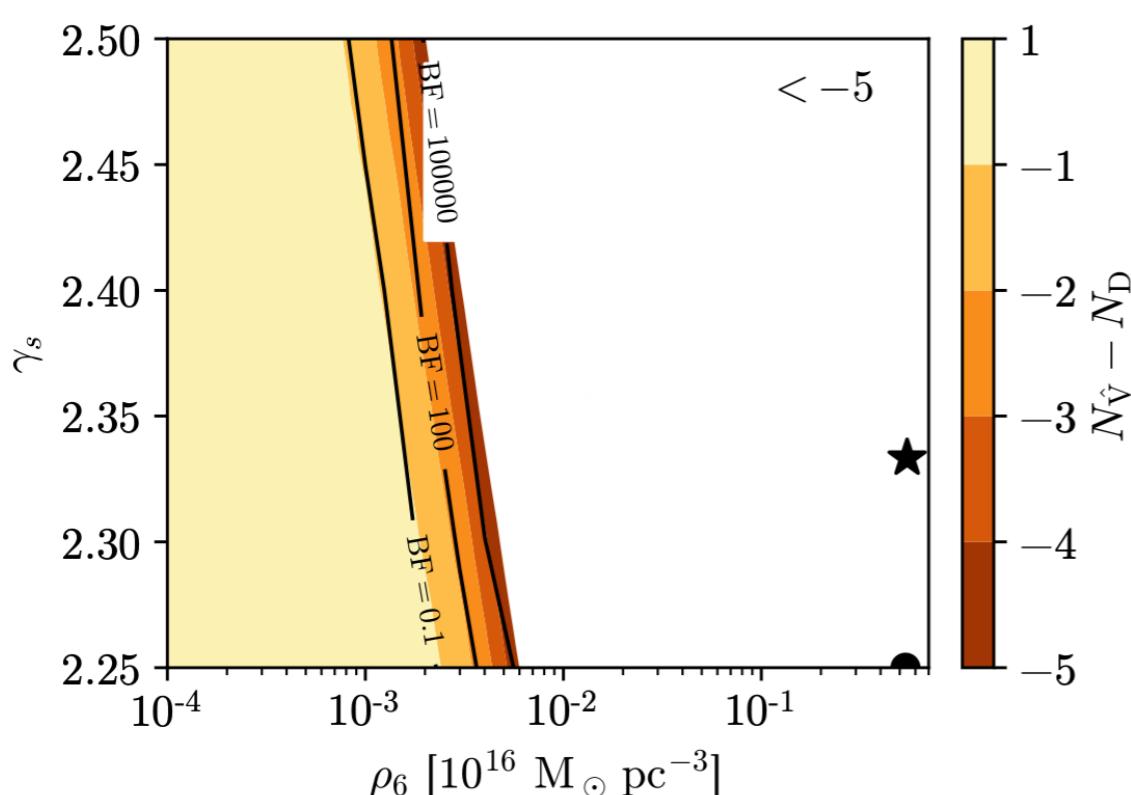


Possible options (?):

- Detect **GW signal close to merger** (where dephasing is small) then ‘track back’ through the data (as dephasing increases)
- Use ‘**generalised inspiral**’ waveforms to parametrise the dephasing
[Chia & Edwards, [2004.06729](#)]
- Use tools from **continuous-wave searches**, breaking the inspiral into ‘chunks’ and looking for quasi-monochromatic signals in each chunk (e.g. Hough transform)
[Guo & Miller, [2205.10359](#)]
- Hybrid of the above?

Conclusions

Detecting collisionless DM spikes would be revolutionary.



In simple models, with simplified searches, it's possible and powerful.

Now we just have a few things left to do...

Towards better spikes

Need to do all of these things accurately, quickly, all at the same time:

Realistic spike
formation scenarios

Accretion (for BHs)

[See Theophanes Karydas'
lightning talk (today)]

Eccentric orbits

[See e.g. Becker et al.,
[2112.09586](#)]

More realistic feedback

Confusion with other
environmental effects

[See Pippa Cole's talk (today)
and Niklas Becker's talk
(tomorrow)]

Relativistic effects

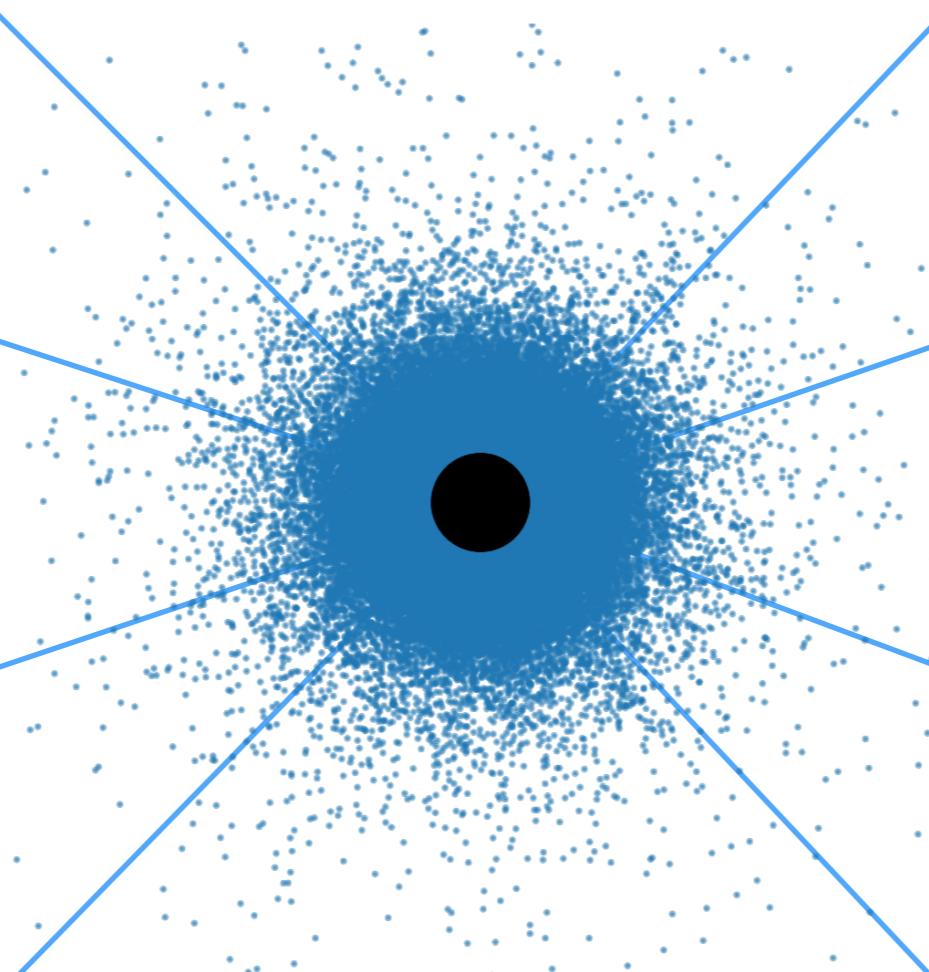
[See e.g. [2204.12508](#) and
Nicholas Sweeney's talk (today)]

Integration with realistic
IMRI/EMRI waveforms

[See e.g. FastEMRIWaveforms,
[2104.04582](#)]

Search strategies

[C.f. Andrea Antonelli's talk
(yesterday)]



Towards better spikes

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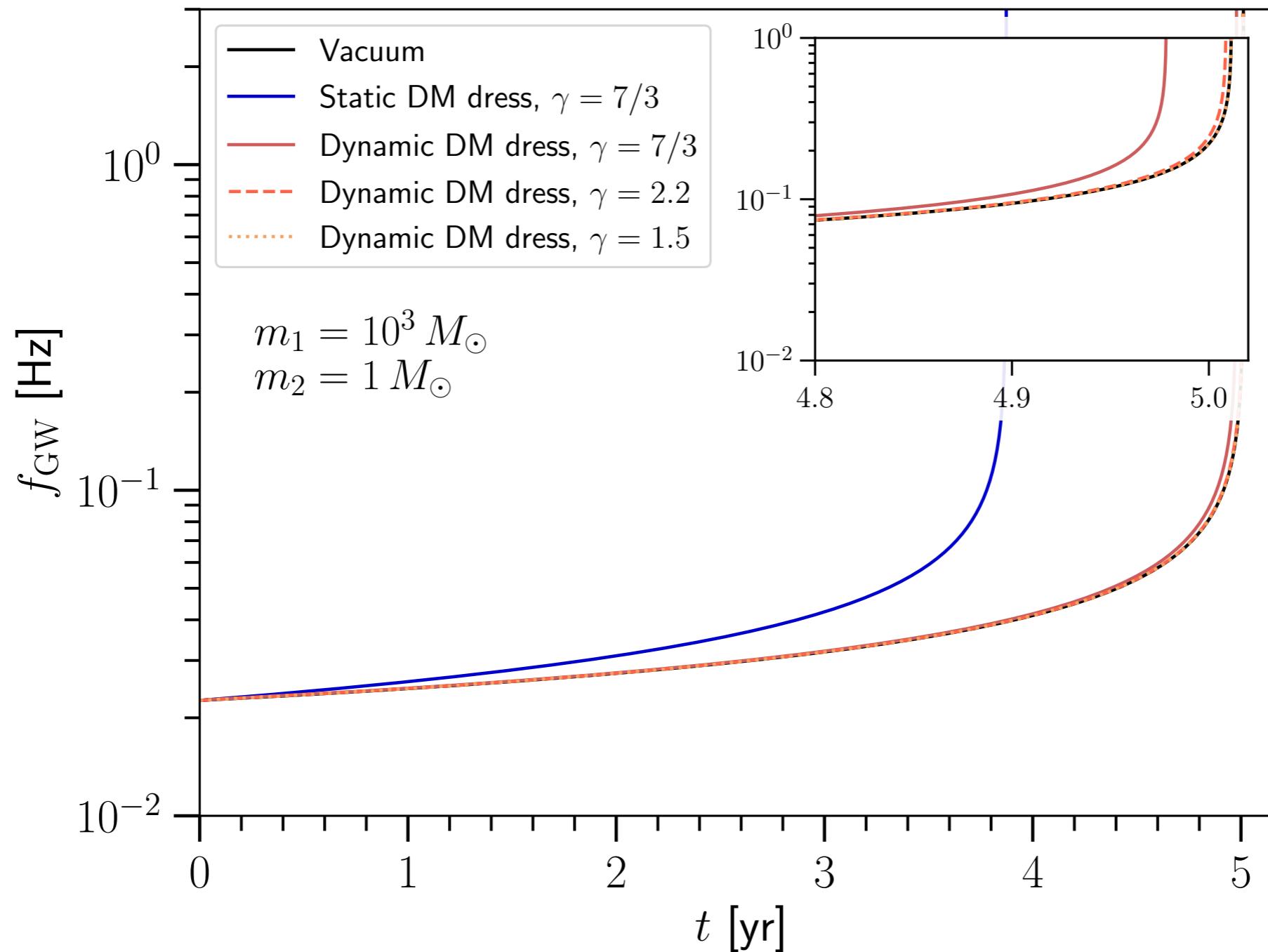
Thank you!

Backup Slides



Time to Merger

Change in time-frequency evolution of the GW inspiral:



‘Dressed’ system mergers ~days earlier than ‘vacuum’ system

Phase space distribution

Follow semi-analytically the phase space distribution of DM:

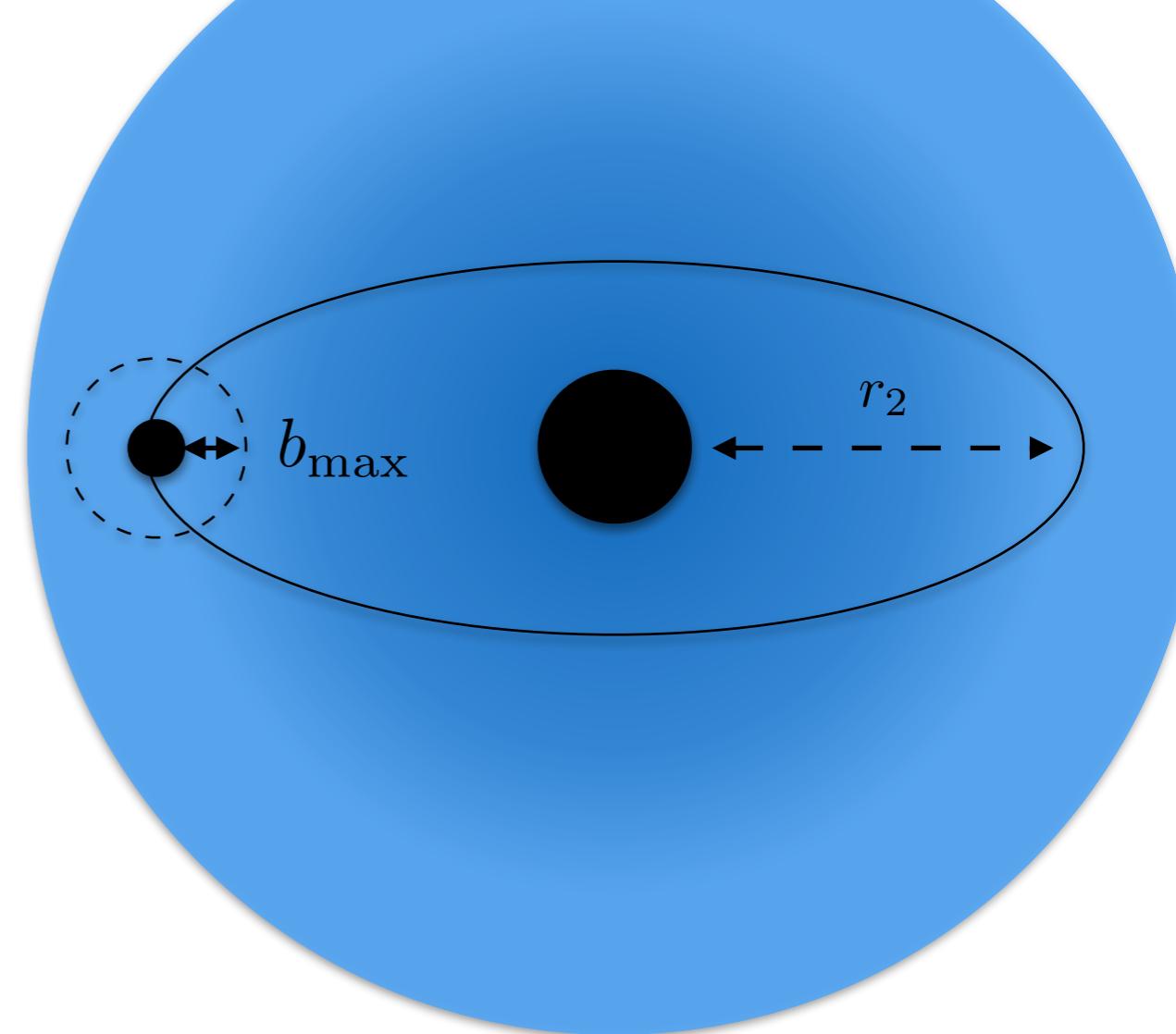
$$f = \frac{dN}{d^3\mathbf{r} d^3\mathbf{v}} \equiv f(\mathcal{E})$$

$$\mathcal{E} = \Psi(r) - \frac{1}{2}v^2$$

Each particle receives a ‘kick’

$$\mathcal{E} \rightarrow \mathcal{E} + \Delta\mathcal{E}$$

through gravitational scattering



Compact object scatters with all DM particles within ‘torus’ of influence over one orbit

Reconstruct density from distribution function:

$$\rho(r) = \int d^3\mathbf{v} f(\mathcal{E})$$

[BJK, Nichols, Gaggero, Bertone, 2002.12811]

[Code available online:
github.com/bradkav/HaloFeedback]

Self-consistent evolution

Assuming everything evolves slowly compared to the orbital period:

$$T_{\text{orb}} \frac{df(\mathcal{E})}{dt} = -p_{\mathcal{E}} f(\mathcal{E}) + \int \left(\frac{\mathcal{E}}{\mathcal{E} - \Delta\mathcal{E}} \right)^{5/2} f(\mathcal{E} - \Delta\mathcal{E}) P_{\mathcal{E}-\Delta\mathcal{E}}(\Delta\mathcal{E}) d\Delta\mathcal{E}$$

$P_{\mathcal{E}}(\Delta\mathcal{E})$ - probability for a particle with energy \mathcal{E} to scatter and receive a 'kick' $\Delta\mathcal{E}$

$p_{\mathcal{E}} = \int P_{\mathcal{E}}(\Delta\mathcal{E}) d\Delta\mathcal{E}$ - total probability for a particle with energy \mathcal{E} to scatter

Self-consistent evolution

Assuming everything evolves slowly compared to the orbital period:

$$T_{\text{orb}} \frac{df(\mathcal{E})}{dt} = -p_{\mathcal{E}} f(\mathcal{E}) + \int \left(\frac{\mathcal{E}}{\mathcal{E} - \Delta\mathcal{E}} \right)^{5/2} f(\mathcal{E} - \Delta\mathcal{E}) P_{\mathcal{E}-\Delta\mathcal{E}}(\Delta\mathcal{E}) d\Delta\mathcal{E}$$

Particles scattering from
 $\mathcal{E} \rightarrow \mathcal{E} + \Delta\mathcal{E}$

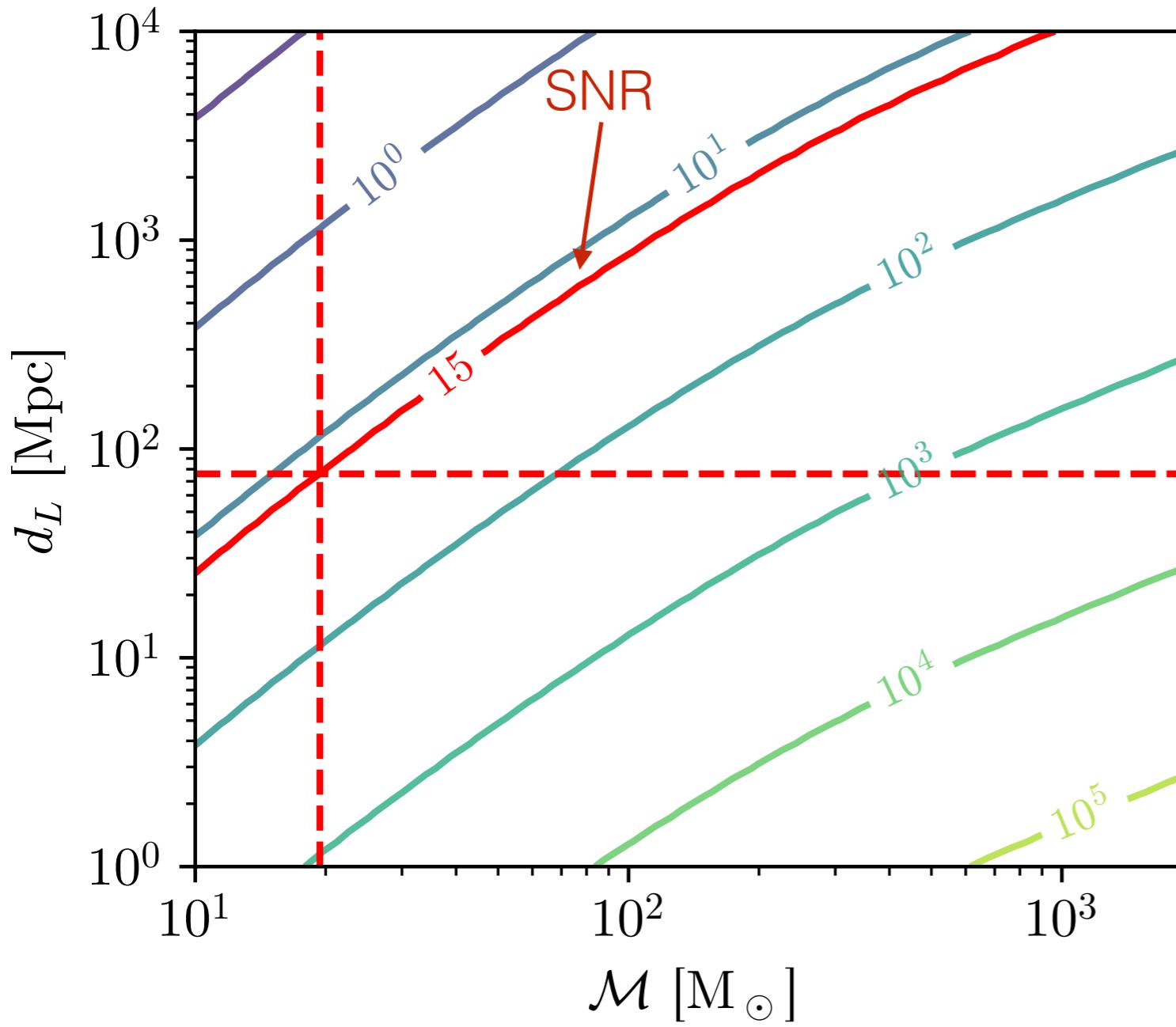
Particles scattering from
 $\mathcal{E} - \Delta\mathcal{E} \rightarrow \mathcal{E}$

$P_{\mathcal{E}}(\Delta\mathcal{E})$ - probability for a particle with energy \mathcal{E} to scatter and receive a 'kick' $\Delta\mathcal{E}$

$p_{\mathcal{E}} = \int P_{\mathcal{E}}(\Delta\mathcal{E}) d\Delta\mathcal{E}$ - total probability for a particle with energy \mathcal{E} to scatter

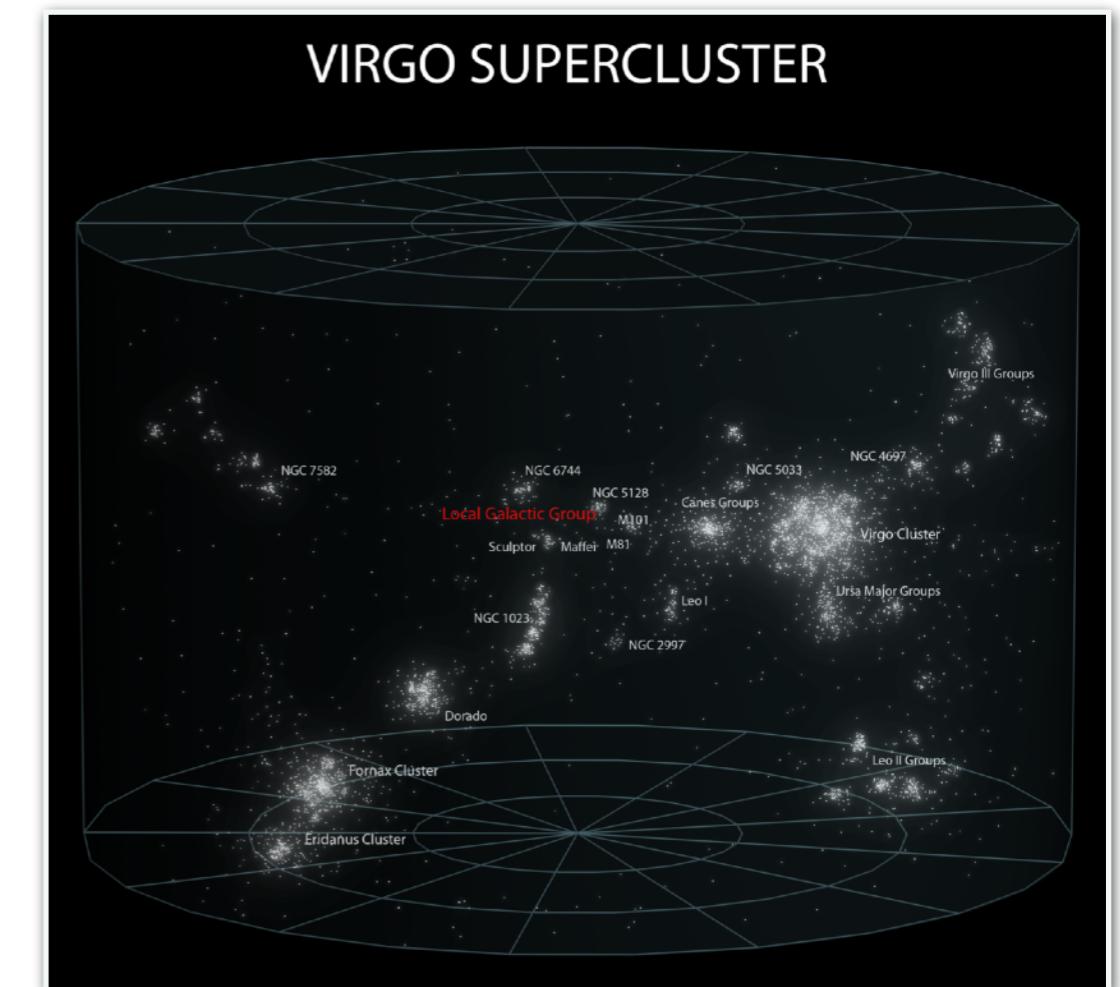
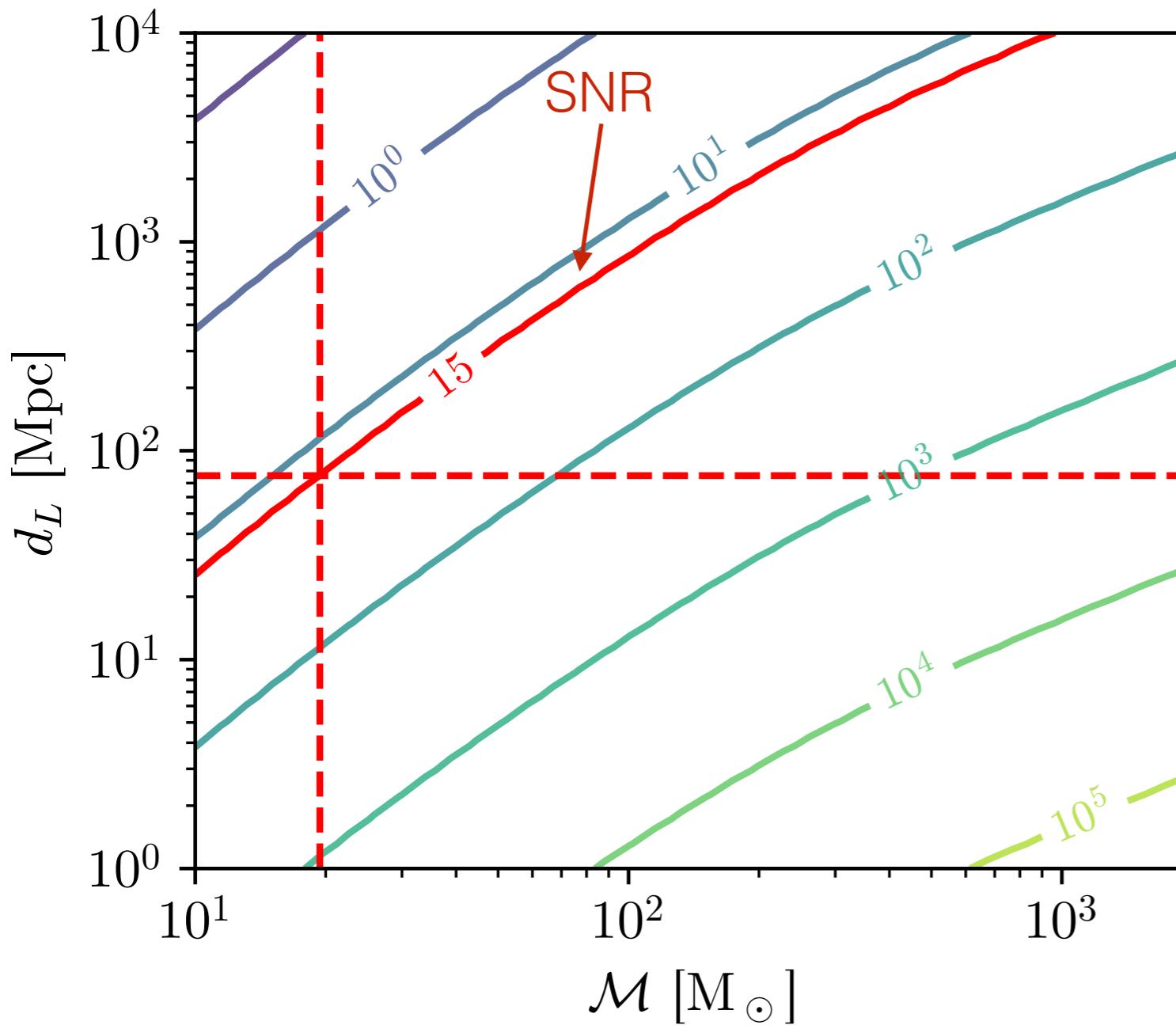
Detectability

Estimate optimal match-filtered SNR for detection with LISA.
(Presence of Dark Dress has almost no impact on SNR):



Detectability

Estimate optimal match-filtered SNR for detection with LISA.
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Multimessenger QCD Axions

